

FACULTY OF ELECTRICAL \& ELECTRONICS ENGINEERING
TEST 2

| COURSE | $:$ | INTELLIGENT CONTROL |
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| COURSE CODE | $:$ | BEE4333 |
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| PROGRAM | $:$ | BEE |

NAME: $\qquad$
STUDENT ID: $\qquad$
NRIC: $\qquad$

INSTRUCTIONS TO CANDIDATES

1. This question paper consists of TWO (2) questions. Answer ALL questions.
2. All the calculations and assumptions must be clearly stated.
3. Write your answers in the exam booklet provided.

## QUESTION 1

Consider the neural network model as shown in Figure 1 with the following assumptions:

- S 1 is a sigmoid activation function and S 2 is a hyperbolic tangent function such that S1: $f(x)=\frac{1}{1+e^{-x}}$ and S2: $f(x)=\frac{e^{x}-e^{-x}}{e^{x}+e^{-x}}$ and the neurons shown as " "" are linear.
- Assume the weights between the layers $i$ and $j\left(w_{j i}\right)$ have an initial value of 0.3 and the weights between the layers $j$ and $k\left(w_{k j}\right)$ have initial value of 0.2 .
- Assume the learning rate, $\eta=0.4$ and momentum, $\alpha=0.9$.
- The inputs are given as follows: $x 1=1, x 2=1, x 3=0$.
- Assume the following notations: $n e t_{j}$ for input of neuron $j, O_{j}$ for output of neuron $j$ and $n e t_{k}$ for input of neuron $k, O_{k}$ for output of neuron $k$ (e.g net ${ }_{k=2}$ for input of neuron $k=2$ )


Figure 1

Answer the following questions:
a) Calculate the value of each of the outputs. $(y 1, y 2, y 3)$.
[8 Marks]
b) Suppose the backpropagation algorithm is used to adapt the weights of the neural network, derive the equation of the weights adaptation between the layers $j$ and $k$ ( $\Delta w_{k j}$ ) [in this case $\boldsymbol{j}=1$ and $\boldsymbol{k}=\mathbf{2}$ ] based on output $\boldsymbol{y} 2$.

Given:

$$
\begin{aligned}
& \Delta w_{k j}=\eta \delta_{k} O_{j} \\
& \Delta w_{k j}(t+1)=\Delta w_{k j}+\alpha \Delta w_{k j}(t) \\
& w_{k j}(t+1)=w_{k j}+\Delta w_{k j}(t+1)
\end{aligned}
$$

where $O_{j}$ is the output of neuron $j, \eta$ is the learning rate and $\delta_{k}$ is the error signal between layers $k$ and $j$ such that:

$$
\begin{aligned}
& \delta_{k}=O_{k}\left(1-O_{k}\right)\left(E_{k}\right) \\
& \delta_{j}=O_{j}\left(1-O_{j}\right) \sum \delta_{k} W_{k j}
\end{aligned}
$$

and where $E_{k}$ is the error between the neural network output ( $y$ ) and the target ( t , such that:

$$
E_{k}=\frac{1}{2}(t-y)^{2}
$$

[6 Marks]
c) Based on the assumptions as given, calculate next value of weight at the branch $(k=2$ and $j=1)$ assuming the target, $\boldsymbol{t}_{2}=\mathbf{0}$.
[8 marks]
d) Suppose hidden layer neuron, $j=1$ is changed to hyperbolic function, $S 2$ :
$f(x)=\frac{e^{x}-e^{-x}}{e^{x}+e^{-x}}$, and neuron, $k=2$ is maintained linear function,
Repeat (a) to calculate the output, $\boldsymbol{y} 2$.
[3 Marks]

## QUESTION 2

(a) Genetic Algorithm (GA) is a part of evolutionary computing that was invented by John Holland.
(i) Draw the GA cycle of reproduction.
[2 Marks]
(ii) Base on (i), explain the working principle of GA.
[3 Marks]
(b) Genetic algorithm (GA) can be used to solve a simple mathematical problem. Consider a mathematical function as shown below:

$$
a+2 b+3 c+4 d=30
$$

Genetic algorithm is used to find the appropriate values of parameter $a, b, c$ and $d$. The chromosome can be represented as:

| a | b | c | d |
| :--- | :--- | :--- | :--- |

To speed up the computation, these 4 (FOUR) parameters are restricted to have integer values between 0 and 30 .

The initial populations are listed in Table 2.1

Table 2.1 Initial Population

| Population <br> Number | $\left[\begin{array}{ll}\text { a b c d }] \\ \hline 1 & {\left[\begin{array}{llll}12 & 05 & 23 & 08\end{array}\right]} \\ \hline 2 & {\left[\begin{array}{lll}01 & 21 & 18\end{array} 03\right.}\end{array}\right]$ |
| :---: | :---: |
| 3 | $\left[\begin{array}{llll}10 & 04 & 13 & 14\end{array}\right]$ |
| 4 | $\left[\begin{array}{llll}2 & 01 & 10 & 06\end{array}\right]$ |

(i) The fitness function is given by

$$
f(x)=a+2 b+3 c+4 d-30
$$

Calculate the fitness value for each population listed in Table 2.1. Arrange from the fittest individual to the less fit individual.
[5 Marks]
(ii) For the $1^{\text {st }}$ generation do the following:
a) Cross the fittest two individuals using one-point crossover at the middle point.
[4 Marks]
b) Suppose the mutation rate, $\rho_{m}=10 \%$, calculate the number of mutations by applying the equation below:

$$
n_{m}=\rho_{m} \times n_{g} \times n_{p}
$$

where $n_{m}, \rho_{m}, n_{g}, n_{p}$ are number of mutations, mutation rate, number of gene in individual and number of populations, respectively.
[2 Marks]
c) Number of mutations obtained from (ii-b) is a number of gene that can be mutated. The number that will be mutated is generated randomly. Suppose that the generated random number is $\mathbf{1 2}$ and $\mathbf{1 8}$, define which individuals that will be mutated.
[2 Marks]
d) Mutate the gene of individuals obtained in (ii-c) with the equation below:

$$
m_{g}=\rho_{m} \times v_{g}
$$

where $m_{g}, \rho_{m}, v_{g}$ are new mutated value, mutation rate and value of original gene, respectively.
[2 Marks]
(iii) Calculate the fitness value for each new population obtained in (ii). (Note : FOUR (4) new population will be generated from (iii)). Evaluate the performance after the FIRST ( $\mathbf{1}^{\text {st }}$ ) generation.
[5 Marks]
[CO3, PO2, C4]

