

Process Monitoring

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Process Monitoring

Chapter 3a

Principal Component Analysis



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Chapter Description

- Aims
 - Understand the basic principles of multivariate techniques.
- Expected Outcomes
 - Comprehensively explain in writing as well as solve mathematically the principles of multivariate analysis based on complex monitoring problem of MSPM framework.
- Other related Information



Subtopics

3.4 Orthogonal Transformation

3.5 Transformation Through Rotation



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3.4 Orthogonal Transformation

Any linear transformation can be represented in matrix form => transforming vectors into vectors (solving simultaneous linear equations):


$$x1^* = a_{11}x1 + a_{21}x2 + \dots + an_1xn$$

$$x2^* = a_{12}x1 + a_{22}x2 + \dots + an_2xn$$

⋮

$$xn^* = a_{1n}x1 + a_{2n}x2 + \dots + annxn$$

Images


$$\mathbf{x}^* = \mathbf{A}\mathbf{x}$$

Pre-images



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3.4 Orthogonal Transformation

- Orthogonal transformation matrix:
 - $\mathbf{A}'\mathbf{A} = \mathbf{A}\mathbf{A}' = \mathbf{I}$
 - The rows and columns of \mathbf{A} are mutually orthogonal and each of unit length
 - Geometrically, it forms a **rotation** (proper or improper) and expressed as sets of direction cosines.



3.5 Transformation Through Rotation

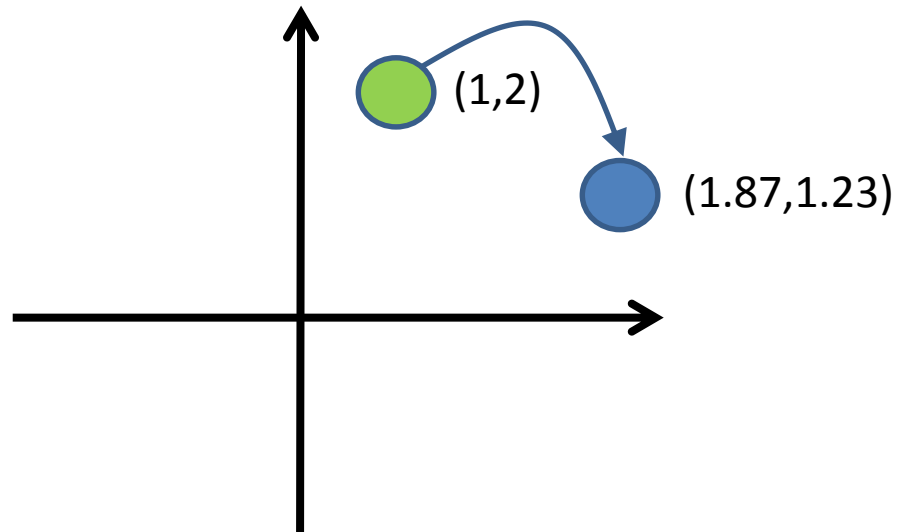
- 2 types of rotation (around the origin):
 1. Point rotation: the points move clockwise or counterclockwise while the basis vectors remained fixed.
 2. Basis vector rotation: the original points remained fixed, while the basis vectors move clockwise or counterclockwise .



3.5 Transformation Through Rotation

Two types of rotation (around the origin):

- i. Point rotation: the points move clockwise or counterclockwise while the basis vectors remained fixed.

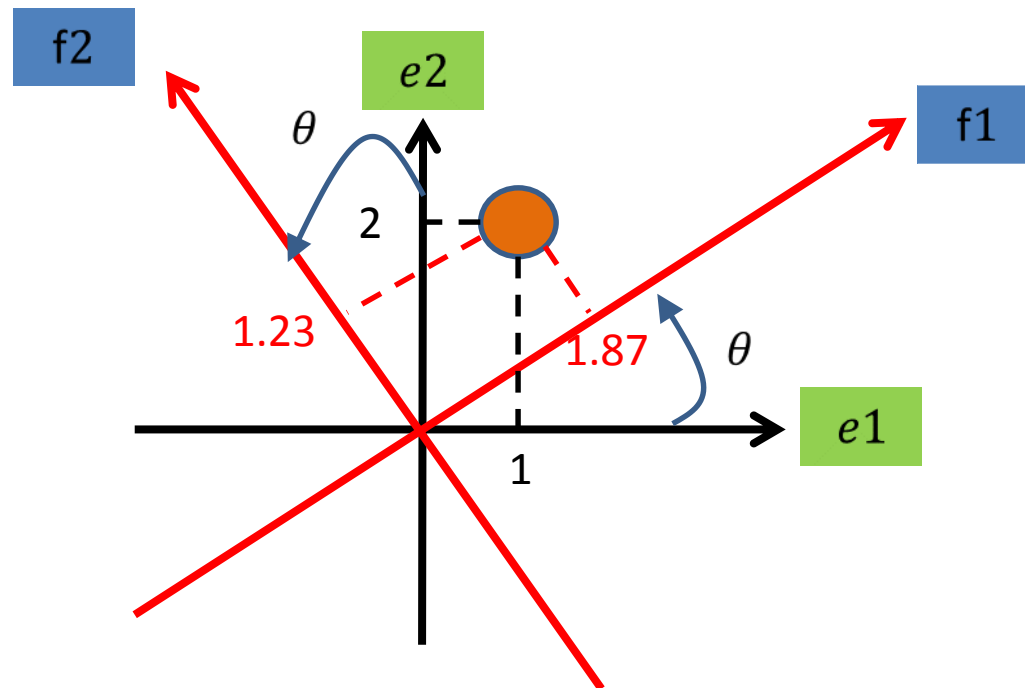


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3.5 Transformation Through Rotation

Two types of rotation...cont.

ii. Basis vector rotation: the original points remained fixed, while the basis vectors move clockwise or counterclockwise



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References

- Green, P.E., and Carroll, J.D., (1976). *Mathematical Tools for Applied Multivariate Analysis*. New York, USA: Academic Press.
- Jackson, J.E., (1991). *A User's Guide To Principal Components*. John Wiley and Sons. USA.



Authors Information

Credit to the authors:



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