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|  Universiti Malaysia PAHANG <small>Engineering • Technology • Creativity</small> FACULTY OF INDUSTRIAL SCIENCES & TECHNOLOGY | SUBJECT: MATHEMATICS FOR MANAGEMENT | | MARKS: |
| | CODE: BUM1123 TOPIC: INEQUALITIES | | |
| | ASSESSMENT: QUIZ | NO: 3 | DUE/DURATION: 10 MINUTES |
| NAME: | | STUDENT ID: | SECTION: |

Choose two from the questions below and solve for x :

$$1) \frac{3x+1}{x+4} \geq 1$$

$$2) \frac{x^2 - 16}{(x-1)^2} < 0$$

$$3) \frac{3x-5}{x} \leq 5-x$$

$$4) \frac{x^2 - 3x - 4}{x^2 - 8x + 16} < 0$$

$$5) \frac{2x+10}{x+3} \geq 1$$

$$6) 1 - \frac{3x}{2x-3} \leq 5$$

$$7) \frac{2x}{x-4} \leq 1$$

$$8) \frac{x+1}{x-6} \geq \frac{x+2}{x-4}$$

$$9) \frac{1}{x+2} > \frac{3}{x+1}$$

$$10) \frac{3}{2-x} > \frac{x}{2+x}$$



| | Answer | Marks | | | | | | | | | | | | | | | | | | | | |
|----------|--|----------------|-------|-----|---|--|---------|---|---|---|--|-------|--|--|--|--|-----|----|-----|-------|-----|--|
| 1 | $\frac{3x+1}{x+4} \geq 1$ $\frac{3x+1}{x+4} - 1 \geq 0$ $\frac{3x+1-(x+4)}{x+4} \geq 0$ $\frac{2x-3}{x+4} \geq 0$ <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$(2x-3)$</td> <td style="border-right: 1px solid black; padding-right: 10px;">-</td> <td style="border-right: 1px solid black; padding-right: 10px;">-</td> <td style="border-right: 1px solid black; padding-right: 10px;">+</td> <td></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 10px;">$(x+4)$</td> <td style="border-right: 1px solid black; padding-right: 10px;">-</td> <td style="border-right: 1px solid black; padding-right: 10px;">+</td> <td style="border-right: 1px solid black; padding-right: 10px;">+</td> <td></td> </tr> <tr> <td colspan="5" style="text-align: center;"><hr/></td> </tr> <tr> <td style="text-align: center;">+ve</td><td style="text-align: center;">-4</td><td style="text-align: center;">-ve</td><td style="text-align: center;">$3/2$</td><td style="text-align: center;">+ve</td></tr> </table> $-\infty < x < -4 \text{ and } \frac{3}{2} \leq x < \infty$ $(-\infty, -4) \text{ and } \left[\frac{3}{2}, \infty\right)$ | $(2x-3)$ | - | - | + | | $(x+4)$ | - | + | + | | <hr/> | | | | | +ve | -4 | -ve | $3/2$ | +ve | M1 A1 M1 A1A1 |
| $(2x-3)$ | - | - | + | | | | | | | | | | | | | | | | | | | |
| $(x+4)$ | - | + | + | | | | | | | | | | | | | | | | | | | |
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| +ve | -4 | -ve | $3/2$ | +ve | | | | | | | | | | | | | | | | | | |
| | | 5 Marks | | | | | | | | | | | | | | | | | | | | |

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| 2 | $$\frac{x^2-16}{(x-1)^2} < 0$$ $$\frac{(x-4)(x+4)}{(x-1)^2} < 0$$ | | | | | | | |---------|----|-----|---|-----|---| | $(x-4)$ | - | - | - | + | | | $(x+4)$ | - | + | + | + | | | $(x-1)$ | - | - | + | + | | | $(x-1)$ | - | - | + | + | | | <hr/> | | | | | | | +ve | -4 | -ve | 1 | -ve | 4 | $$-4 < x < 1 \text{ and } 1 < x < 4$$ $$(-4, 1) \text{ and } (1, 4)$$ | **M1** **A1** **M1** **A1A1** |
| | | **5 Marks** |


| | | |
|---|---|------------------------|
| 3 | $\frac{3x-15}{x} \leq 5-x$ $\frac{3x-15}{x} - 5 + x \leq 0$ $\frac{3x-15-5x+x^2}{x} \leq 0$ $\frac{x^2-2x-15}{x} \leq 0$ $\frac{(x-5)(x+3)}{x} \leq 0$ | M1 A1 |
| | $\begin{array}{c ccccc c} (x-5) & & - & & - & & + \\ (x+3) & & - & & + & & + \\ x & & - & & - & & + \\ \hline & -ve & -3 & +ve & 0 & -ve & 5 & +ve \end{array}$ | M1 |
| | $(-\infty, -3] \text{ and } (0, 5]$ | |
| | A1A1 | |
| | 5 Marks | |

| | | |
|---|--|-----------|
| 4 | $\frac{x^2-3x-4}{x^2-8x+16} < 0$ $\frac{(x+1)(x-4)}{(x-4)(x-4)} < 0$ $\frac{(x+1)}{(x-4)} < 0$ | M1 |
| | $\begin{array}{c ccccc c} (x+1) & & - & & + & & + \\ (x-4) & & - & & - & & + \\ \hline & +ve & -1 & -ve & 4 & +ve & \end{array}$ | A1 |
| | $(-1, 4]$ | |
| | M1 A1A1 | |
| | 5 Marks | |



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|---------|---|---------|-----|----|-----|---------|---|---|---|-------|--|--|--|--|-----|----|-----|----|-----|--|
| 5 | $\frac{2x+10}{x+3} \geq 1$ $\frac{2x+10}{x+3} - 1 \geq 0$ $\frac{2x+10-x-3}{x+3} \geq 0$ $\frac{x+7}{x+3} \geq 0$ <table border="1" style="width: 100%; text-align: center;"> <tr> <td>$(x+7)$</td><td>-</td><td>+</td><td>+</td></tr> <tr> <td>$(x+3)$</td><td>-</td><td>-</td><td>+</td></tr> <tr> <td colspan="4"><hr/></td></tr> <tr> <td></td><td>+ve</td><td>-7</td><td>-ve</td><td>-3</td><td>+ve</td></tr> </table> $(-\infty, -7] \text{ and } (-3, \infty)$ | $(x+7)$ | - | + | + | $(x+3)$ | - | - | + | <hr/> | | | | | +ve | -7 | -ve | -3 | +ve | M1 A1 M1 A1A1 5 Marks |
| $(x+7)$ | - | + | + | | | | | | | | | | | | | | | | | |
| $(x+3)$ | - | - | + | | | | | | | | | | | | | | | | | |
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| | +ve | -7 | -ve | -3 | +ve | | | | | | | | | | | | | | | |

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|-------------|--|-------------|-----|-----|-----|----------|---|---|---|-------|--|--|--|--|-----|------|-----|-----|-----|--|
| 6 | $1 - \frac{3x}{2x-3} \leq 5$ $1 - 5 - \frac{3x}{2x-3} \leq 0$ $-4 - \frac{3x}{2x-3} \leq 0$ $\frac{-8x-3x+12}{2x-3} \leq 0$ $\frac{-11x+12}{2x-3} \leq 0$ <table border="1" style="width: 100%; text-align: center;"> <tr> <td>$(-11x+12)$</td><td>+</td><td>-</td><td>-</td></tr> <tr> <td>$(2x-3)$</td><td>-</td><td>-</td><td>+</td></tr> <tr> <td colspan="4"><hr/></td></tr> <tr> <td></td><td>-ve</td><td>1.09</td><td>+ve</td><td>1.5</td><td>-ve</td></tr> </table> $(-\infty, 1.09] \text{ and } (1.5, \infty)$ | $(-11x+12)$ | + | - | - | $(2x-3)$ | - | - | + | <hr/> | | | | | -ve | 1.09 | +ve | 1.5 | -ve | M1 A1 M1 A1A1 5 Marks |
| $(-11x+12)$ | + | - | - | | | | | | | | | | | | | | | | | |
| $(2x-3)$ | - | - | + | | | | | | | | | | | | | | | | | |
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| | -ve | 1.09 | +ve | 1.5 | -ve | | | | | | | | | | | | | | | |



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|-----------|--|----------------|-----|----|-----|----|-----|---------|---|---|---|---|---|---------|---|---|---|---|---|--|-----|------|-----|----|-----|----|-----|--|
| 7 | $\frac{1}{x+2} > \frac{3}{x+1}$ $\frac{1}{x+2} - \frac{3}{x+1} > 0$ $\frac{(x+1) - 3(x+2)}{(x+1)(x+2)} > 0$ $\frac{-2x-5}{(x+1)(x+2)} > 0$ <table border="1" style="width: 100%; text-align: center;"> <tr> <td>$(-2x-5)$</td><td>+</td><td>-</td><td>-</td><td>-</td><td>-</td></tr> <tr> <td>$(x+1)$</td><td>-</td><td>-</td><td>-</td><td>-</td><td>+</td></tr> <tr> <td>$(x+2)$</td><td>-</td><td>-</td><td>+</td><td>-</td><td>+</td></tr> <tr> <td></td><td>+ve</td><td>-2.5</td><td>-ve</td><td>-2</td><td>+ve</td><td>-1</td><td>-ve</td></tr> </table> $(-\infty, -2.5] \text{ and } (-2, -1)$ | $(-2x-5)$ | + | - | - | - | - | $(x+1)$ | - | - | - | - | + | $(x+2)$ | - | - | + | - | + | | +ve | -2.5 | -ve | -2 | +ve | -1 | -ve | M1 A1 M1 A1A1 |
| $(-2x-5)$ | + | - | - | - | - | | | | | | | | | | | | | | | | | | | | | | | |
| $(x+1)$ | - | - | - | - | + | | | | | | | | | | | | | | | | | | | | | | | |
| $(x+2)$ | - | - | + | - | + | | | | | | | | | | | | | | | | | | | | | | | |
| | +ve | -2.5 | -ve | -2 | +ve | -1 | -ve | | | | | | | | | | | | | | | | | | | | | |
| | | 5 Marks | | | | | | | | | | | | | | | | | | | | | | | | | | |

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|---------|--|----------------|-----|---|-----|---|-----|---------|---|---|---|---|---|---------|---|---|---|---|---|--|-----|----|-----|---|-----|---|-----|--|
| 8 | $\frac{x+1}{x-6} \geq \frac{x+2}{x-4}$ $\frac{x+1}{x-6} - \frac{x+2}{x-4} \geq 0$ $\frac{(x+1)(x-4) - (x+2)(x-6)}{(x-6)(x-4)} \geq 0$ $\frac{x+8}{(x+1)(x+2)} \geq 0$ <table border="1" style="width: 100%; text-align: center;"> <tr> <td>$(x+8)$</td><td>-</td><td>+</td><td>+</td><td>-</td><td>+</td></tr> <tr> <td>$(x-6)$</td><td>-</td><td>-</td><td>-</td><td>-</td><td>+</td></tr> <tr> <td>$(x-4)$</td><td>-</td><td>-</td><td>+</td><td>-</td><td>+</td></tr> <tr> <td></td><td>-ve</td><td>-8</td><td>+ve</td><td>4</td><td>-ve</td><td>6</td><td>+ve</td></tr> </table> $(-8, 4) \text{ and } (6, \infty)$ | $(x+8)$ | - | + | + | - | + | $(x-6)$ | - | - | - | - | + | $(x-4)$ | - | - | + | - | + | | -ve | -8 | +ve | 4 | -ve | 6 | +ve | M1 A1 M1 A1A1 |
| $(x+8)$ | - | + | + | - | + | | | | | | | | | | | | | | | | | | | | | | | |
| $(x-6)$ | - | - | - | - | + | | | | | | | | | | | | | | | | | | | | | | | |
| $(x-4)$ | - | - | + | - | + | | | | | | | | | | | | | | | | | | | | | | | |
| | -ve | -8 | +ve | 4 | -ve | 6 | +ve | | | | | | | | | | | | | | | | | | | | | |
| | | 5 Marks | | | | | | | | | | | | | | | | | | | | | | | | | | |



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|---------|----|---|---------|-----|---|---|---|---------|---|---|---|---|-------|--|--|--|--|-----|----|-----|---|-----|--|
| | 9 | $\frac{2x}{x-4} \leq 1$ $\frac{2x}{x-4} - 1 \leq 0$ $\frac{2x}{x-4} - \frac{x-4}{x-4} \leq 0$ $\frac{2x-x+4}{x-4} \leq 0$ $\frac{x+4}{x-4} \leq 0$ <table style="margin-left: auto; margin-right: auto;"> <tr> <td>$(x+4)$</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">-</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td></tr> <tr> <td>$(x-4)$</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">-</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">-</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td></tr> <tr> <td colspan="5" style="text-align: center;"><hr/></td></tr> <tr> <td style="padding-left: 10px;">+ve</td><td style="padding-left: 10px;">-4</td><td style="padding-left: 10px;">-ve</td><td style="padding-left: 10px;">4</td><td style="padding-left: 10px;">+ve</td></tr> </table> $(-4, 4]$ | $(x+4)$ | - | + | + | + | $(x-4)$ | - | - | + | + | <hr/> | | | | | +ve | -4 | -ve | 4 | +ve | |
| $(x+4)$ | - | + | + | + | | | | | | | | | | | | | | | | | | | |
| $(x-4)$ | - | - | + | + | | | | | | | | | | | | | | | | | | | |
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| +ve | -4 | -ve | 4 | +ve | | | | | | | | | | | | | | | | | | | |
| | | M1 | | | | | | | | | | | | | | | | | | | | | |
| | | A1 | | | | | | | | | | | | | | | | | | | | | |
| | | M1M1 | | | | | | | | | | | | | | | | | | | | | |
| | | A1 | | | | | | | | | | | | | | | | | | | | | |
| | | 5 Marks | | | | | | | | | | | | | | | | | | | | | |

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|-----------------|----|--|-----------------|-----|---|---|---|---------|---|---|---|---|---------|---|---|---|---|-------|--|--|--|--|-----|----|-----|---|-----|--|
| | 10 | $\frac{3}{2-x} > \frac{x}{2+x}$ $\frac{3}{2-x} - \frac{x}{2+x} > 0$ $\frac{3(2+x) - x(2-x)}{(2-x)(2+x)} > 0$ $\frac{x^2 + x + 6}{(2-x)(2+x)} > 0$ <table style="margin-left: auto; margin-right: auto;"> <tr> <td>$(x^2 + x + 6)$</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td></tr> <tr> <td>$(2-x)$</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">-</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">-</td></tr> <tr> <td>$(2+x)$</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">-</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td><td style="border-left: 1px solid black; border-right: 1px solid black; padding: 0 5px;">+</td></tr> <tr> <td colspan="5" style="text-align: center;"><hr/></td></tr> <tr> <td style="padding-left: 10px;">-ve</td><td style="padding-left: 10px;">-2</td><td style="padding-left: 10px;">+ve</td><td style="padding-left: 10px;">2</td><td style="padding-left: 10px;">-ve</td></tr> </table> $(-2, 2)$ | $(x^2 + x + 6)$ | + | + | + | + | $(2-x)$ | + | + | - | - | $(2+x)$ | - | + | + | + | <hr/> | | | | | -ve | -2 | +ve | 2 | -ve | |
| $(x^2 + x + 6)$ | + | + | + | + | | | | | | | | | | | | | | | | | | | | | | | | |
| $(2-x)$ | + | + | - | - | | | | | | | | | | | | | | | | | | | | | | | | |
| $(2+x)$ | - | + | + | + | | | | | | | | | | | | | | | | | | | | | | | | |
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| -ve | -2 | +ve | 2 | -ve | | | | | | | | | | | | | | | | | | | | | | | | |
| | | M1 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | A1 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | M1M1 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | A1 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | 5 Marks | | | | | | | | | | | | | | | | | | | | | | | | | | |

