

ENGINEERING MECHANICS

BAA1113

Chapter 2: Force Vectors (Static)

by

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Chapter Description

- Aims
 - To review the Parallelogram Law and Trigonometry
 - To explain the Force Vectors
 - To explain the Vectors Operations (Parlaw & Cartesian)
 - To express force and position in Cartesian Vectors
- Expected Outcomes
 - Able to solve the problems of force and position vectors in the mechanics applications by using Cartesian Coordinate System
- References
 - Russel C. Hibbeler. Engineering Mechanics: Statics & Dynamics, 14th Edition

Chapter Outline

- 2.1 Scalars and Vectors – part I
- 2.2 Vectors Operations – part I
- 2.3 Vectors Addition of Forces – part I
- 2.4 Cartesian Vectors – part II
- 2.5 **Force and Position Vectors – part III**

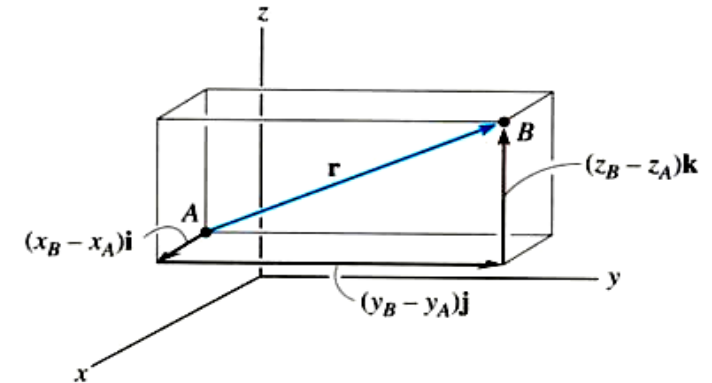


2.5 Position Vector



- **B** is the **ending point** and **A** is the **starting point**
- Must **subtract** the **tail** coordinates **from** the **tip**

What is Position Vector?



- It is a **fixed vector** that locates a **point in space** relative to another **point**
- A Position can be defined by its **coordinate in 3-D space**
- A **Position vector** directed from A to B is denoted as r_{AB}
- Let point A (X_A, Y_A, Z_A) and B (X_B, Y_B, Z_B)

$$r_{AB} = \{(X_B - X_A) i + (Y_B - Y_A) j + (Z_B - Z_A) k\}m$$

Application of Position Vector

Measure the **length** of cable AB

Magnitude **r** represent the **length** of cable

Unit vector $\mathbf{u} = \mathbf{r}/r$



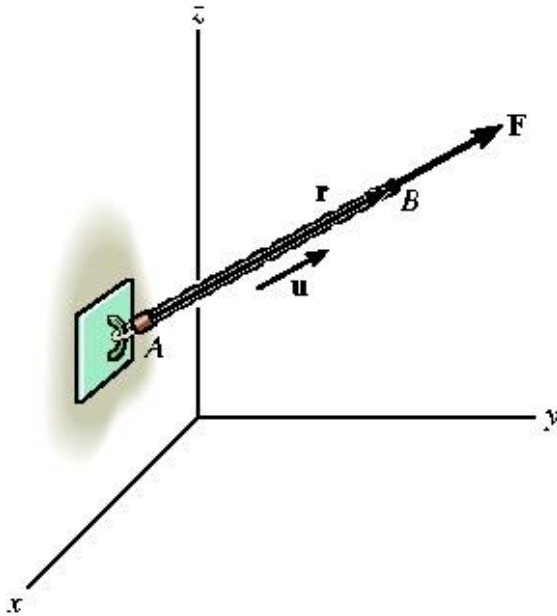
Position vector \mathbf{r} can be established

$$\mathbf{r} = x\mathbf{i} + y\mathbf{j} + z\mathbf{k}$$

Measure the **direction** of cable AB

Angles α, β, γ represent the **direction** of cable AB

Force Vector Directed Along a Line

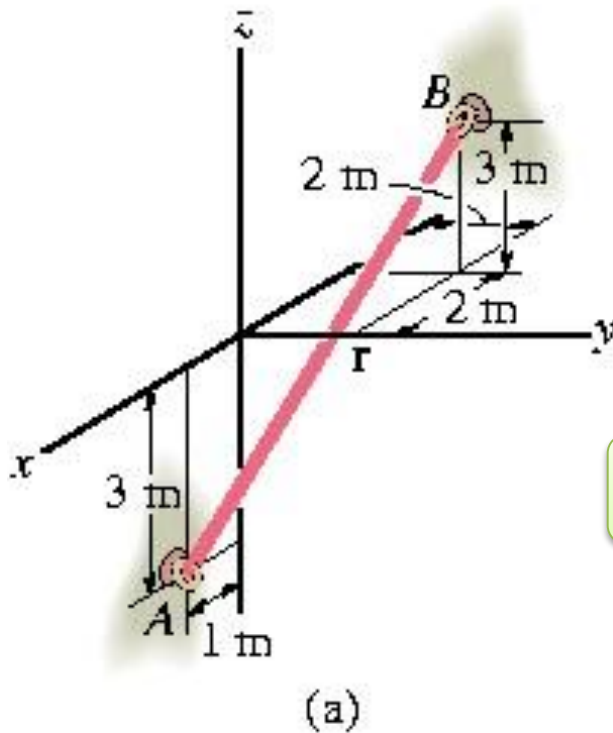


If a **force** is directed along a **line**

- It can represent the force vector in **Cartesian coordinates** by using a **unit vector** and the **force's magnitude**
- Step 1: Established position vector \mathbf{r}_{AB}
- Step 2: Established unit vector $\mathbf{u}_{AB} = (\mathbf{r}_{AB} / r_{AB})$
- Step 3: Magnitude of force $\mathbf{F} = F \mathbf{u}_{AB}$

Example 2.12

The elastic rubber band is attached to points A and B. Determine the length and direction measured from A to B



Step 1

- Established position vector r_{AB}

Step 2

- Established unit vector $u_{AB} = (r_{AB} / r_{AB})$

Magnitude r_{AB} = length of the rubber band

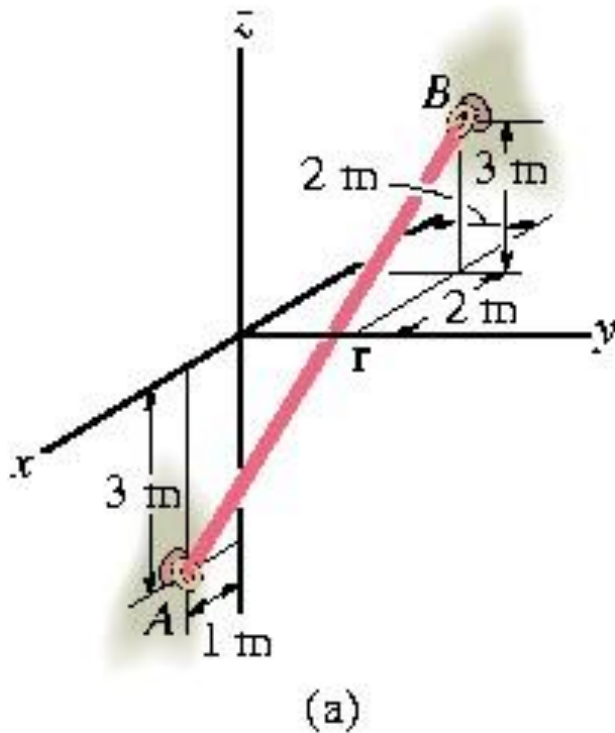
Step 3

Direction = coordinate angles of r_{AB}

$$u_{AB} = \cos \alpha \mathbf{i} + \cos \beta \mathbf{j} + \cos \gamma \mathbf{k}$$

Solution Example 2.12

The elastic rubber band is attached to points A and B. Determine the length and direction measured from A to B



Step 1

- Established position vector r_{AB}

- From A to B, it's need to go -3 m in the x-direction, 2 m in the y-direction, and 6 m in the z-direction

$$r_{AB} = \{-3 \mathbf{i} + 2 \mathbf{j} + 6 \mathbf{k}\} \text{m}$$

or

- point A (X_A, Y_A, Z_A) and B (X_B, Y_B, Z_B)
- point A (1, 0, -3) and B (-2, 2, 3)

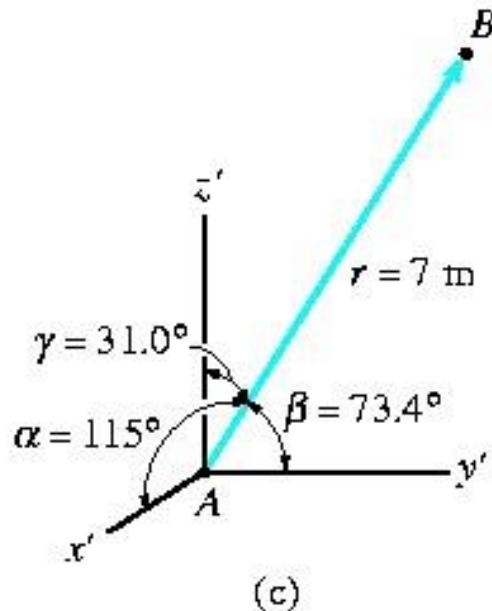
$$r_{AB} = \{(X_B - X_A) \mathbf{i} + (Y_B - Y_A) \mathbf{j} + (Z_B - Z_A) \mathbf{k}\} \text{m}$$

$$r_{AB} = \{(-2 - 1) \mathbf{i} + (2 - 0) \mathbf{j} + (3 - (-3)) \mathbf{k}\} \text{m}$$

$$r_{AB} = \{(-3) \mathbf{i} + (2) \mathbf{j} + (6) \mathbf{k}\} \text{m}$$

Solution Example 2.12

The elastic rubber band is attached to points A and B. Determine the length and direction measured from A to B



Step 2

- Established unit vector $\mathbf{u}_{AB} = (\mathbf{r}_{AB}/r_{AB})$

$$r_{AB} = \sqrt{(-3)^2 + (2)^2 + (6)^2} = 7\text{m}$$

Magnitude = length of the rubber band = 7m

$$\mathbf{u}_{AC} = (-3/7) \mathbf{i} + (2/7) \mathbf{j} + (6/7) \mathbf{k} \} \text{N}$$

$$\mathbf{u}_{AC} = -0.428 \mathbf{i} + 0.285 \mathbf{j} + 0.857 \mathbf{k} \} \text{N}$$

- Direction A to B

$$\mathbf{u}_{AB} = \cos \alpha \mathbf{i} + \cos \beta \mathbf{j} + \cos \gamma \mathbf{k}$$

$$\alpha = \cos^{-1}(-3/7) = 115^\circ$$

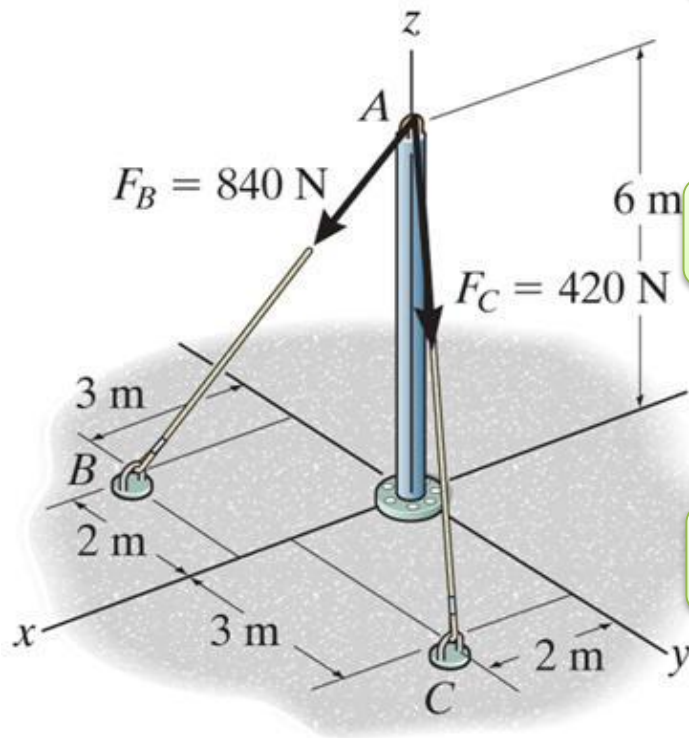
$$\beta = \cos^{-1}(2/7) = 73.4^\circ$$

$$\gamma = \cos^{-1}(6/7) = 31^\circ$$

Step 3

Example 2.13

Determine the force \mathbf{F}_{AC} in the Cartesian vectors. Given , the 420 N Force along the cable **AC**



Step 1

- Established position vector \mathbf{r}_{AC}

Step 2

- Established unit vector $\mathbf{u}_{AC} = (\mathbf{r}_{AC} / r_{AC})$

Step 3

- Magnitude of force $\mathbf{F} = F \mathbf{u}_{AC}$

Solution Example 2.13

Determine the force \mathbf{F}_{AC} in the Cartesian vectors. Given , the 420 N Force along the cable **AC**

Step 1

- Established position vector \mathbf{r}_{AC}
- From A to C, it's need to go 2 m in the x-direction, 3 m in the y-direction, and -6 m in the z-direction

$$\mathbf{r}_{AC} = \{2\mathbf{i} + 3\mathbf{j} - 6\mathbf{k}\}\text{m}$$

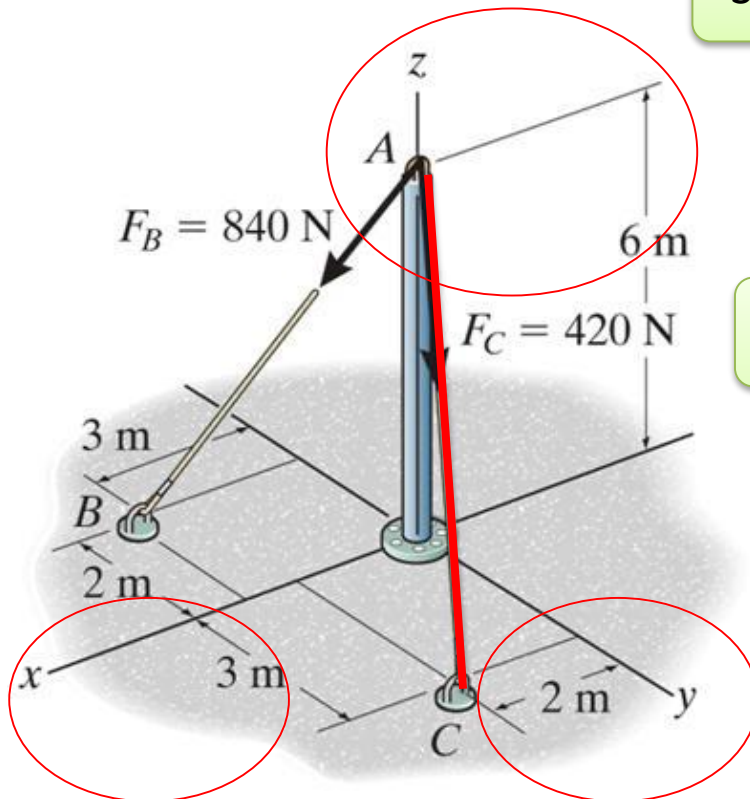
or

- point A (X_A, Y_A, Z_A) and C (X_C, Y_C, Z_C)
- point A (0, 0, 6) and C (2, 3, 0)

$$\mathbf{r}_{AC} = \{(X_C - X_A)\mathbf{i} + (Y_C - Y_A)\mathbf{j} + (Z_C - Z_A)\mathbf{k}\}\text{m}$$

$$\mathbf{r}_{AC} = \{(2 - 0)\mathbf{i} + (3 - 0)\mathbf{j} + (0 - 6)\mathbf{k}\}\text{m}$$

$$\mathbf{r}_{AC} = \{(2)\mathbf{i} + (3)\mathbf{j} + (-6)\mathbf{k}\}\text{m}$$



Solution Example 2.13

Determine the force \mathbf{F}_{AC} in the Cartesian vectors. Given , the 420 N Force along the cable **AC**

Step 2

- Established unit vector $\mathbf{u}_{AC} = (\mathbf{r}_{AC}/r_{AC})$

$$r_{AC} = \sqrt{(2)^2 + (3)^2 + (-6)^2} = 7\text{ m}$$

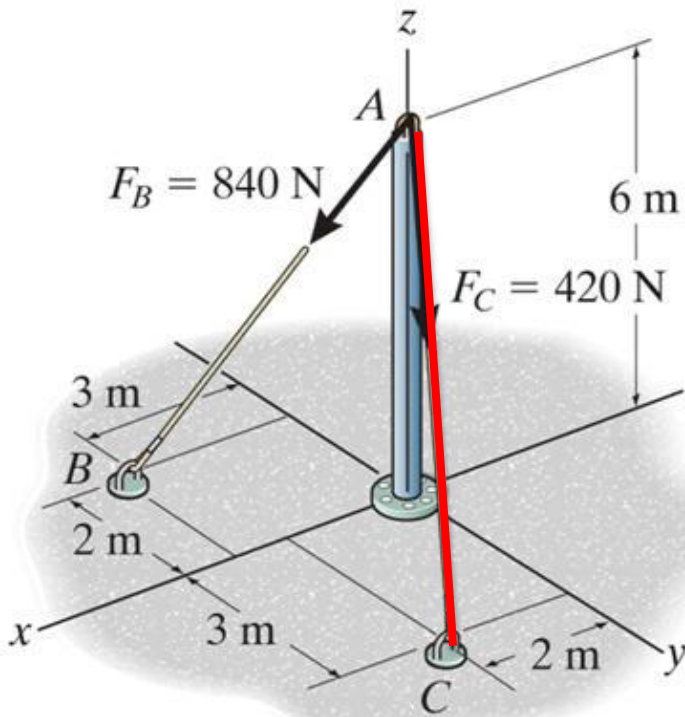
Step 3

- Magnitude of force $\mathbf{F} = F \mathbf{u}_{AC}$

$$\mathbf{F} = 420\text{ N } \mathbf{u}_{AC}$$

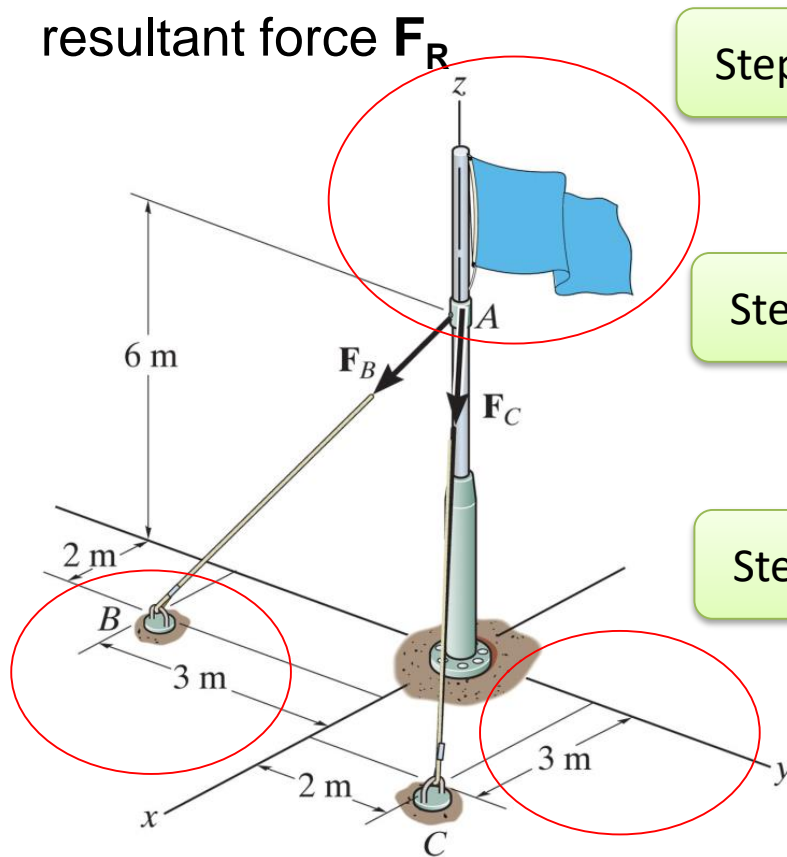
$$\mathbf{F}_{AC} = 420\{ (2 \mathbf{i} + 3 \mathbf{j} - 6 \mathbf{k}) / 7 \} \text{ N}$$

$$\mathbf{F}_{AC} = \{ \underline{120} \mathbf{i} + \underline{180} \mathbf{j} - \underline{360} \mathbf{k} \} \text{ N}$$



Example 2.14

Two forces are acting on the flag pole which $F_B = 560\text{N}$ and $F_C = 700\text{N}$. Determine the magnitude and coordinate direction angles of the resultant force \mathbf{F}_R



Step 1

- Established position vector

$$\mathbf{r}_{AB}$$

$$\mathbf{r}_{AC}$$

Step 2

- Established unit vector

$$\mathbf{u}_{AB} = (\mathbf{r}_{AB} / r_{AB})$$

$$\mathbf{u}_{AC} = (\mathbf{r}_{AC} / r_{AC})$$

Step 3

- Magnitude of force $F_{AB} = F_{AB} / u_{AB}$

$$F_{AC} = F_{AC} / u_{AC}$$

- Add the two forces to get \mathbf{F}_R

- Calculate the magnitude and direction of \mathbf{F}_R

Example 2.14

Two forces are acting on the flag pole which $F_B = 560\text{N}$ and $F_C = 700\text{N}$. Determine the magnitude and coordinate direction angles of the resultant force F_R

Step 1

- Established position vector

$$r_{AB} = \{2\mathbf{i} - 3\mathbf{j} - 6\mathbf{k}\} \text{ m}$$

$$r_{AC} = \{3\mathbf{i} + 2\mathbf{j} - 6\mathbf{k}\} \text{ m}$$

Step 2

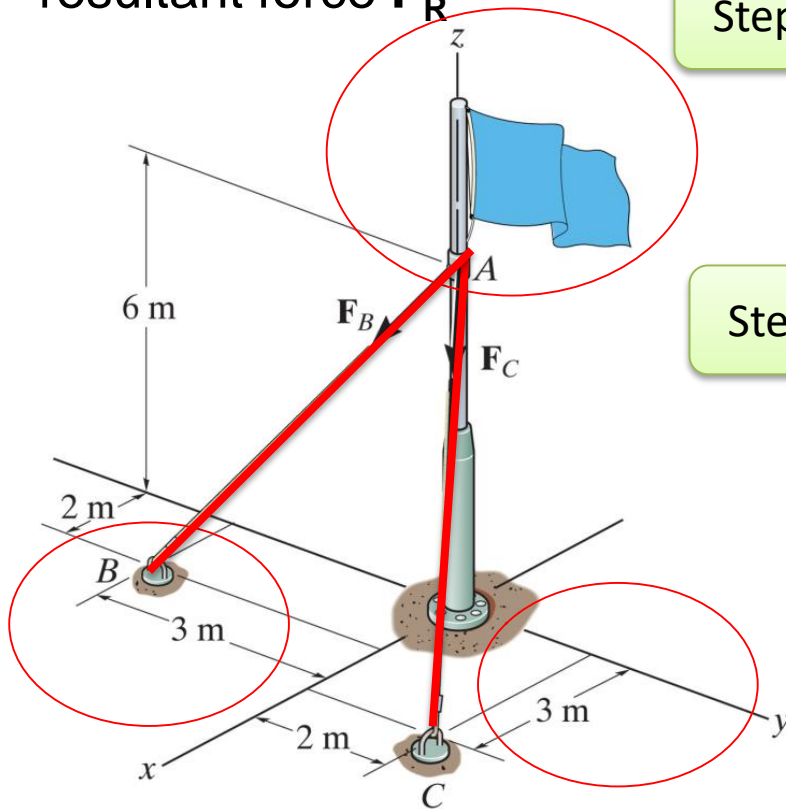
- Established unit vector

$$u_{AB} = (r_{AB} / r_{AB})$$

$$r_{AB} = \sqrt{(2)^2 + (-3)^2 + (-6)^2} = 7\text{ m}$$

$$u_{AC} = (r_{AC} / r_{AC})$$

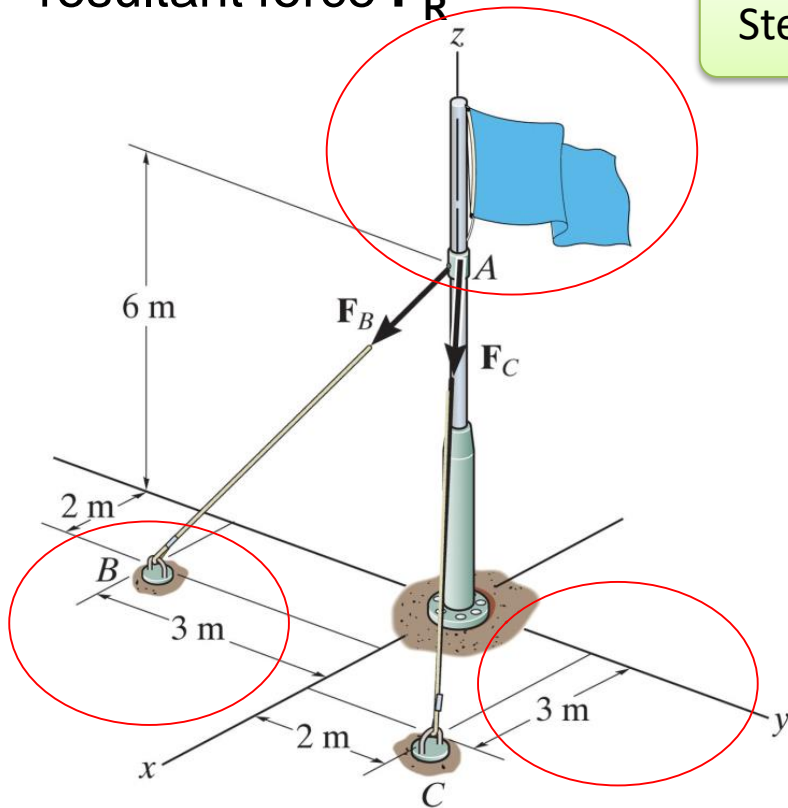
$$r_{AC} = \sqrt{(3)^2 + (2)^2 + (-6)^2} = 7\text{ m}$$



Example 2.14

Two forces are acting on the flag pole which $F_B = 560\text{N}$ and $F_C = 700\text{N}$. Determine the magnitude and coordinate direction angles of the resultant force F_R

Step 3



- Magnitude of force

$$F_{AB} = F_{AB} / u_{AB}$$

$$F_{AB} = 560 (r_{AB} / r_{AB}) \text{ N}$$

$$F_{AB} = 560 (2 \mathbf{i} - 3 \mathbf{j} - 6 \mathbf{k}) / 7 \text{ N}$$

$$F_{AB} = (160 \mathbf{i} - 240 \mathbf{j} - 480 \mathbf{k}) \text{ N}$$

$$F_{AC} = F_{AC} / u_{AC}$$

$$F_{AC} = 700 (r_{AC} / r_{AC}) \text{ N}$$

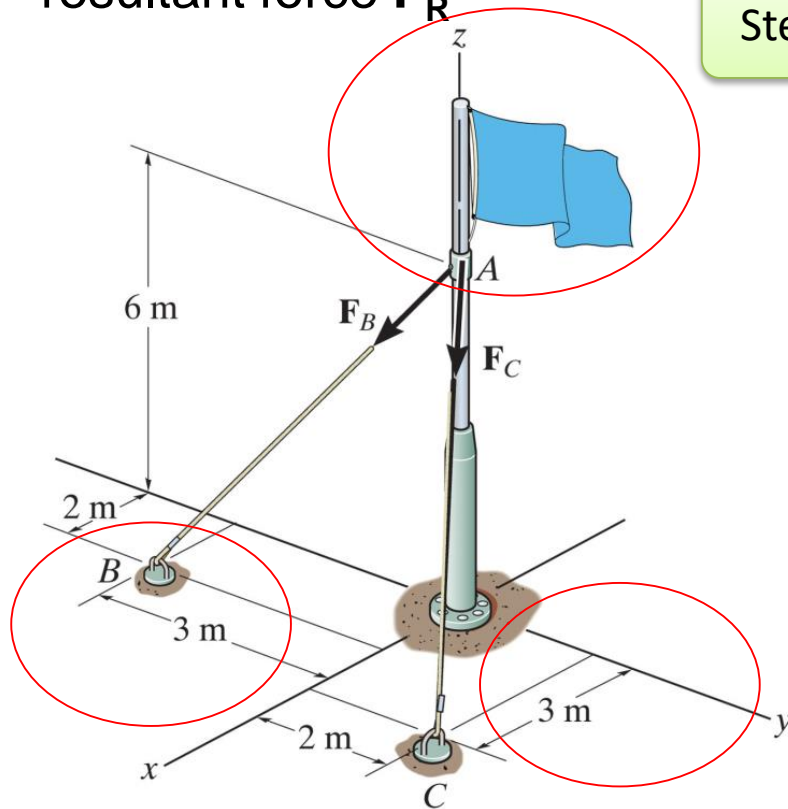
$$F_{AC} = 700 (3 \mathbf{i} + 2 \mathbf{j} - 6 \mathbf{k}) / 7 \text{ N}$$

$$F_{AC} = \{300 \mathbf{i} + 200 \mathbf{j} - 600 \mathbf{k}\} \text{ N}$$

Example 2.14

Two forces are acting on the flag pole which $F_B = 560\text{N}$ and $F_C = 700\text{N}$. Determine the magnitude and coordinate direction angles of the resultant force \mathbf{F}_R

Step 3



- Magnitude of \mathbf{F}_R

$$\mathbf{F}_{AB} = (160 \mathbf{i} - 240 \mathbf{j} - 480 \mathbf{k}) \text{ N}$$

$$\mathbf{F}_{AC} = \{300 \mathbf{i} + 200 \mathbf{j} - 600 \mathbf{k}\} \text{ N}$$

$$\mathbf{F}_R = \mathbf{F}_{AB} + \mathbf{F}_{AC}$$

$$= \{460 \mathbf{i} - 40 \mathbf{j} - 1080 \mathbf{k}\} \text{ N}$$

$$F_R = \sqrt{(460)^2 + (-40)^2 + (-1080)^2} = 1174.5 \text{ N}$$

$$\mathbf{F}_R = 1175 \text{ N}$$

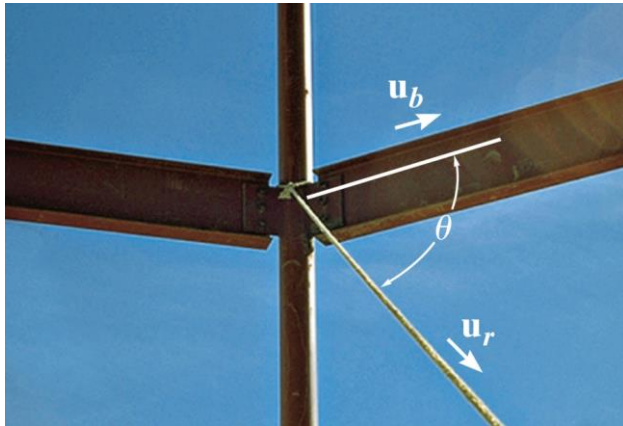
- Direction angles of \mathbf{F}_R

$$\alpha = \cos^{-1}(460/1175) = \underline{66.9^\circ}$$

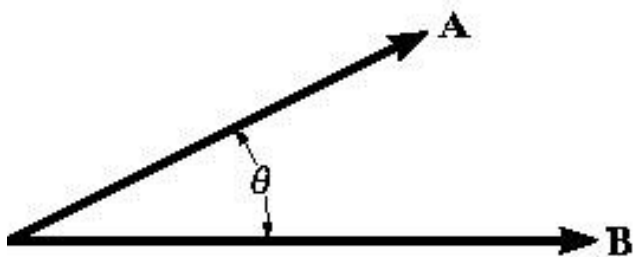
$$\beta = \cos^{-1}(-40/1175) = \underline{92.0^\circ}$$

$$\gamma = \cos^{-1}(-1080/1175) = \underline{157^\circ}$$

Dot Product



- A **dot product** of vectors **A** and **B** can be defined by $\mathbf{A} \cdot \mathbf{B} = AB \cos \theta$
- Use to determine the **angle between two vectors** and its magnitude
- Its angle θ is the smallest angle between the two vectors and is always in a range of 0° to 180°
- The result of **dot product** is a **scalar** (\pm Number)
- Units of the dot product will be the product of the **units** of the **A** and **B** vectors

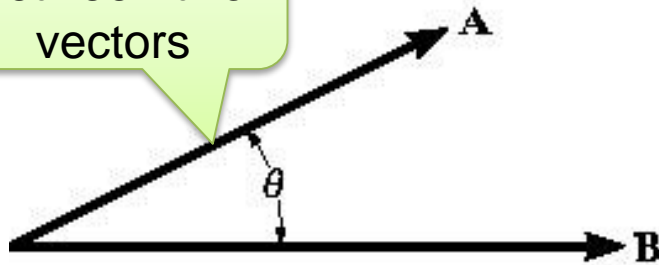


$$\mathbf{i} \cdot \mathbf{j} = 0 \text{ \& \ } \mathbf{i} \cdot \mathbf{i} = 1$$

$$\begin{aligned} \mathbf{A} \cdot \mathbf{B} &= (A_x \mathbf{i} + A_y \mathbf{j} + A_z \mathbf{k}) \cdot (B_x \mathbf{i} + B_y \mathbf{j} + B_z \mathbf{k}) \\ &= A_x B_x + A_y B_y + A_z B_z \end{aligned}$$

Application of Dot Product

Angle
between two
vectors

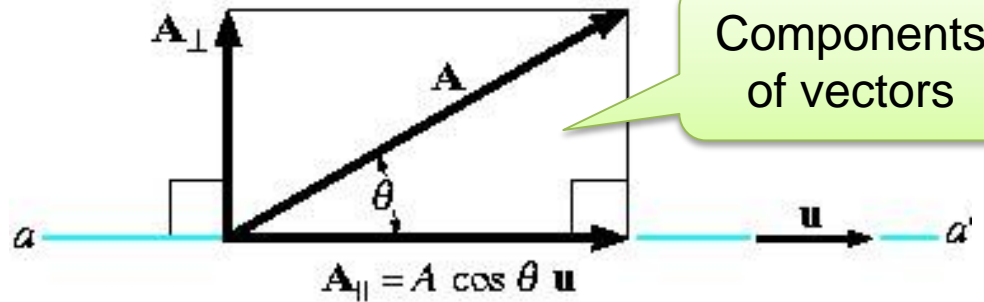


- The angle formed between two vectors or intersecting lines

$$\theta = \cos^{-1} [(A \cdot B) / (AB)]$$

$$0^\circ \leq \theta \leq 180^\circ$$

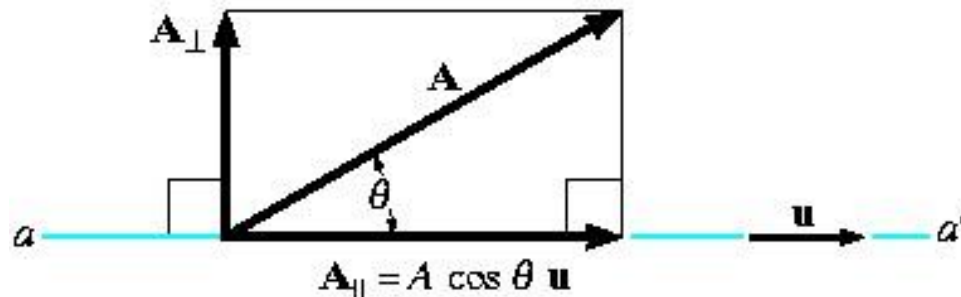
Note: if $A \cdot B = 0$, $\cos^{-1} 0 = 90^\circ$,
A is perpendicular to **B**



- The components of a vector parallel and perpendicular to a line
- Component of **A** parallel or collinear with line aa' is defined by A_{\parallel} (projection of **A** onto the line)
$$A_{\parallel} = A \cos \theta$$
- If direction of line is specified by unit vector **u** ($u = 1$),
$$A_{\parallel} = A \cos \theta = \mathbf{A} \cdot \mathbf{u}$$

Application of Dot Product

- If A_{\parallel} is positive, \mathbf{A}_{\parallel} has a directional sense same as \mathbf{u}
- If A_{\parallel} is negative, \mathbf{A}_{\parallel} has a directional sense opposite to \mathbf{u}
- \mathbf{A}_{\parallel} expressed as a vector
$$\mathbf{A}_{\parallel} = A \cos \theta \mathbf{u}$$
$$= (\mathbf{A} \cdot \mathbf{u}) \mathbf{u}$$



Application of Dot Product

For component of \mathbf{A} perpendicular to line aa'

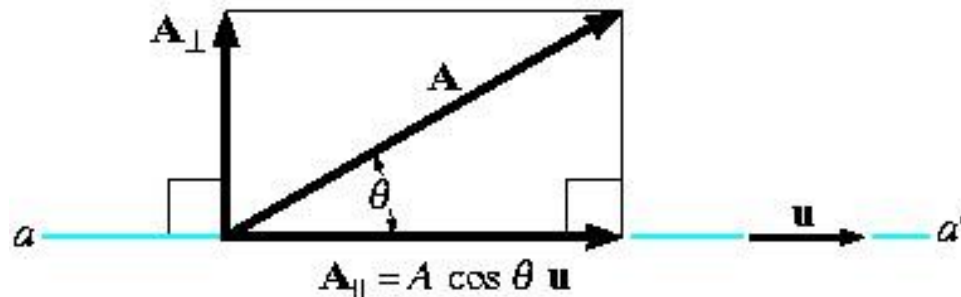
1. Since $\mathbf{A} = \mathbf{A}_{\parallel} + \mathbf{A}_{\perp}$,

then $\mathbf{A}_{\perp} = \mathbf{A} - \mathbf{A}_{\parallel}$

2. $\theta = \cos^{-1} [(\mathbf{A} \cdot \mathbf{u}) / (A)]$

then $\mathbf{A}_{\perp} = A \sin \theta$

3. If \mathbf{A}_{\parallel} is known, by Pythagorean Theorem



Law of Operation of Dot Product

1. Commutative law

$$\mathbf{A} \cdot \mathbf{B} = \mathbf{B} \cdot \mathbf{A}$$

2. Multiplication by a scalar

$$a(\mathbf{A} \cdot \mathbf{B}) = (a\mathbf{A}) \cdot \mathbf{B} = \mathbf{A} \cdot (a\mathbf{B}) = (\mathbf{A} \cdot \mathbf{B})a$$

3. Distribution law

$$\mathbf{A} \cdot (\mathbf{B} + \mathbf{D}) = (\mathbf{A} \cdot \mathbf{B}) + (\mathbf{A} \cdot \mathbf{D})$$

Law of Operation of Dot Product

■ Cartesian Vector Formulation

- Dot product of Cartesian unit vectors

Eg: $\mathbf{i} \cdot \mathbf{i} = (1)(1)\cos 0^\circ = 1$ and

$$\mathbf{i} \cdot \mathbf{j} = (1)(1)\cos 90^\circ = 0$$

- Similarly

$$\mathbf{i} \cdot \mathbf{i} = 1 \quad \mathbf{j} \cdot \mathbf{j} = 1 \quad \mathbf{k} \cdot \mathbf{k} = 1$$

$$\mathbf{i} \cdot \mathbf{j} = 0 \quad \mathbf{i} \cdot \mathbf{k} = 0 \quad \mathbf{j} \cdot \mathbf{k} = 0$$

Law of Operation of Dot Product

■ Cartesian Vector Formulation

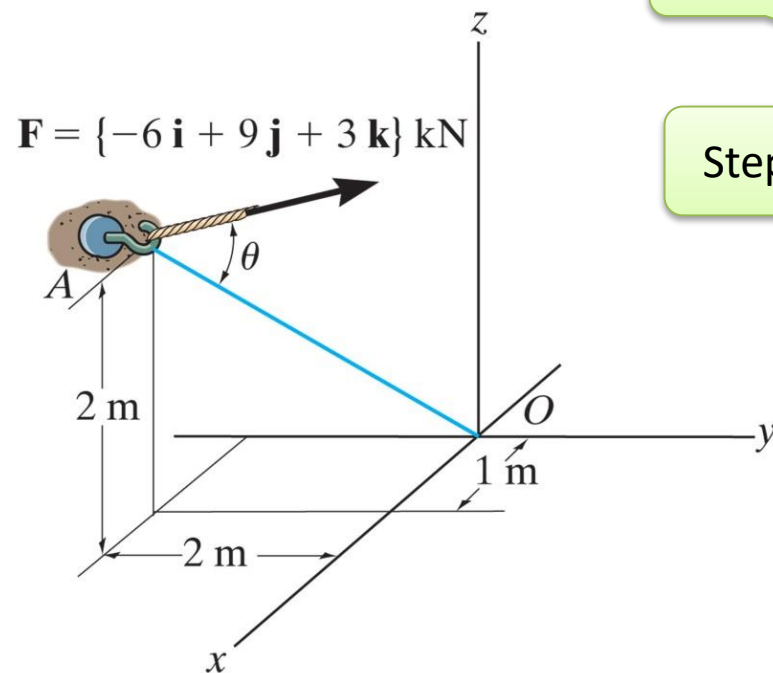
- Dot product of 2 vectors **A** and **B**

$$\begin{aligned}\mathbf{A} \cdot \mathbf{B} &= (A_x \mathbf{i} + A_y \mathbf{j} + A_z \mathbf{k}) \cdot (B_x \mathbf{i} + B_y \mathbf{j} + B_z \mathbf{k}) \\ &= A_x B_x (\mathbf{i} \cdot \mathbf{i}) + A_x B_y (\mathbf{i} \cdot \mathbf{j}) + A_x B_z (\mathbf{i} \cdot \mathbf{k}) \\ &\quad + A_y B_x (\mathbf{j} \cdot \mathbf{i}) + A_y B_y (\mathbf{j} \cdot \mathbf{j}) + A_y B_z (\mathbf{j} \cdot \mathbf{k}) \\ &\quad + A_z B_x (\mathbf{k} \cdot \mathbf{i}) + A_z B_y (\mathbf{k} \cdot \mathbf{j}) + A_z B_z (\mathbf{k} \cdot \mathbf{k}) \\ &= A_x B_x + A_y B_y + A_z B_z\end{aligned}$$

Note: since result is a scalar, be careful of including any unit vectors in the result

Example 2.15

The force are acting on the hook at point A. Determine the angle between the force and the line AO, and the magnitude of the projection of force along the line AO



Step 1

- Established position vector

$$\mathbf{r}_{AO}$$

Step 2

- Established dot product

$$\mathbf{F} \cdot \mathbf{r}_{AO}$$

$$\theta = \cos^{-1}\left\{\frac{\mathbf{F} \cdot \mathbf{r}_{AO}}{F r_{AO}}\right\}$$

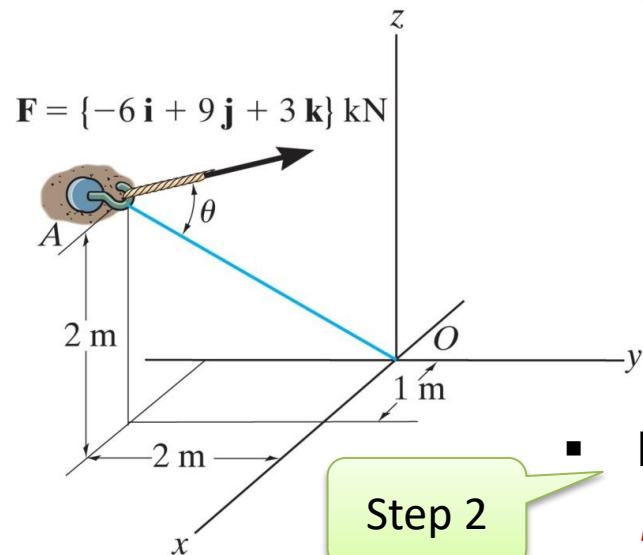
Step 3

- Magnitude of the projection of force, F_{AO}

$$F_{AO} = \mathbf{F} \cdot \mathbf{u}_{AO} \text{ or } F \cos \theta$$

Solution Example 2.15

The force are acting on the hook at point A. Determine the angle between the force and the line AO, and the magnitude of the projection of force along the line AO



Step 1

- Established position vector

$$\mathbf{r}_{AO} = \{-1 \mathbf{i} + 2 \mathbf{j} - 2 \mathbf{k}\} \text{ m}$$

$$r_{AO} = \sqrt{(-1)^2 + (2)^2 + (-2)^2} = 3 \text{ m}$$

$$\mathbf{F} = \{-6 \mathbf{i} + 9 \mathbf{j} + 3 \mathbf{k}\} \text{ kN}$$

$$F = \sqrt{(-6)^2 + (9)^2 + (3)^2} = 11.22 \text{ m}$$

Step 2

- Established dot product

$$\mathbf{i} \cdot \mathbf{j} = 0 \text{ \& } \mathbf{i} \cdot \mathbf{i} = 1$$

$$\mathbf{F} \cdot \mathbf{r}_{AO} = A_x B_x + A_y B_y + A_z B_z$$

$$\mathbf{F} \cdot \mathbf{r}_{AO} = (-6)(-1) + (9)(2) + (3)(-2) = 18 \text{ kN}\cdot\text{m}$$

$$\theta = \cos^{-1}\{(\mathbf{F} \cdot \mathbf{r}_{AO}) / (F r_{AO})\}$$

$$\theta = \cos^{-1}\{18 / (11.22 \times 3)\} = \underline{57.67^\circ}$$

Solution Example 2.15

Step 3

- Magnitude of the projection of force, F_{AO}

$$F_{AO} = \mathbf{F} \cdot \mathbf{u}_{AO} \quad \text{or} \quad F \cos \theta$$

$$\mathbf{u}_{AO} = \mathbf{r}_{AO} / r_{AO} = (-1/3) \mathbf{i} + (2/3) \mathbf{j} + (-2/3) \mathbf{k}$$

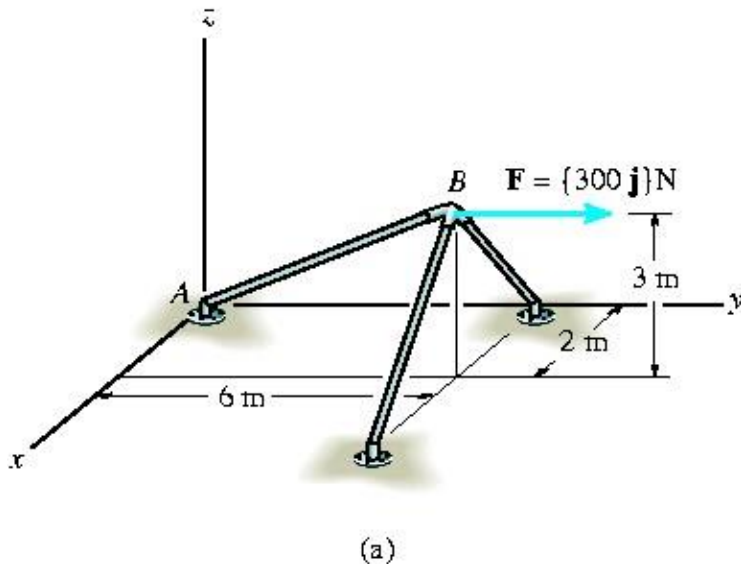
$$F_{AO} = \mathbf{F} \cdot \mathbf{u}_{AO} = (-6)(-1/3) + (9)(2/3) + (3)(-2/3) = \underline{6.00 \text{ kN}}$$

or

$$F_{AO} = F \cos \theta = 11.22 \cos (57.67^\circ) = \underline{6.00 \text{ kN}}$$

Example 2.16

The frame is subjected to a horizontal force, $\mathbf{F} = \{300\mathbf{j}\}$ at point B. Determine the components of this force parallel and perpendicular to the member AB



Step 1

- Established position vector

\mathbf{u}_B

Step 2

- Established dot product

$$F_{AB} = F \cos \theta = \mathbf{F} \cdot \mathbf{u}_B$$

Step 3

Express in Cartesian form:

- Parallel component
- Perpendicular component

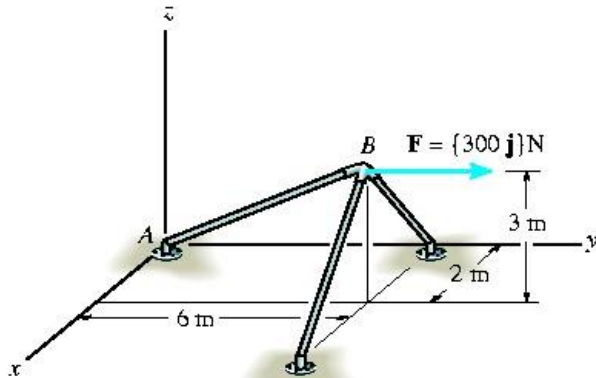
Step 4

$$\mathbf{A} = \mathbf{A}_{\parallel} + \mathbf{A}_{\perp},$$

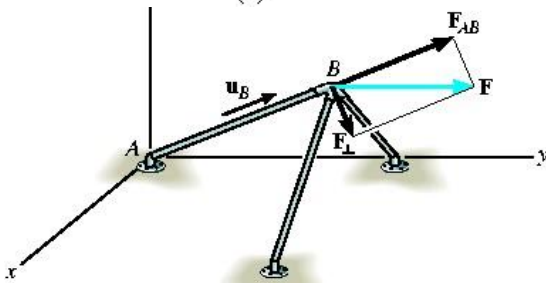
then $\mathbf{A}_{\perp} = \mathbf{A} - \mathbf{A}_{\parallel}$

Solution Example 2.16

The frame is subjected to a horizontal force, $\mathbf{F} = \{300\mathbf{j}\}$ at point B. Determine the components of this force parallel and perpendicular to the member AB



(a)



(b)

Step 1

- Established position & unit vector

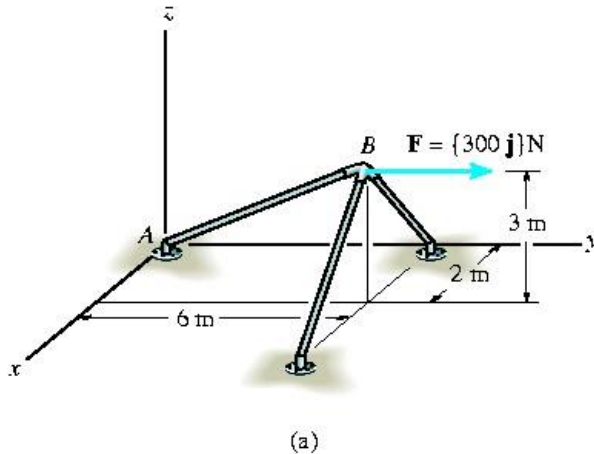
$$\begin{aligned}\vec{u}_B &= \frac{\vec{r}_B}{|\vec{r}_B|} = \frac{2\vec{i} + 6\vec{j} + 3\vec{k}}{\sqrt{(2)^2 + (6)^2 + (3)^2}} \\ &= 0.286\vec{i} + 0.857\vec{j} + 0.429\vec{k}\end{aligned}$$

Step 2, dot product

$$\begin{aligned}|\vec{F}_{AB}| &= |\vec{F}| \cos \theta \\ &= \vec{F} \cdot \vec{u}_B = (300\vec{j}) \cdot (0.286\vec{i} + 0.857\vec{j} + 0.429\vec{k}) \\ &= (0)(0.286) + (300)(0.857) + (0)(0.429) \\ &= 257.1\text{N}\end{aligned}$$

Solution Example 2.16

The frame is subjected to a horizontal force, $\mathbf{F} = \{300\mathbf{j}\}$ at point B. Determine the components of this force parallel and perpendicular to the member AB



Step 3

Since result is a positive scalar, \mathbf{F}_{AB} has the same sense of direction as \mathbf{u}_{AB} .

Express in Cartesian form:

$$\begin{aligned}\vec{F}_{AB} &= |\vec{F}_{AB}| \vec{u}_{AB} \\ &= (257.1\text{N}) (0.286\vec{i} + 0.857\vec{j} + 0.429\vec{k}) \\ &= \{73.5\vec{i} + 220\vec{j} + 110\vec{k}\}\text{N}\end{aligned}$$

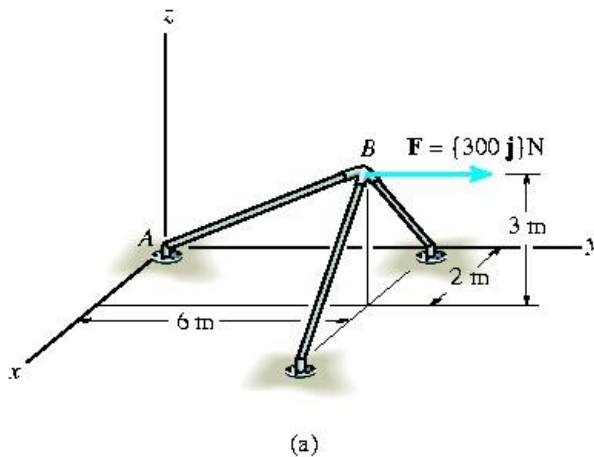
Step 4

Perpendicular component

$$\begin{aligned}\vec{F}_{\perp} &= \vec{F} - \vec{F}_{AB} = 300\vec{j} - (73.5\vec{i} + 220\vec{j} + 110\vec{k}) \\ &= \{-73.5\vec{i} + 80\vec{j} - 110\vec{k}\}\text{N}\end{aligned}$$

Solution Example 2.16

The frame is subjected to a horizontal force, $\mathbf{F} = \{300\mathbf{j}\}$ at point B. Determine the components of this force parallel and perpendicular to the member AB



Step 5

Magnitude can be determined
From \mathbf{F}_\perp or from Pythagorean
Theorem

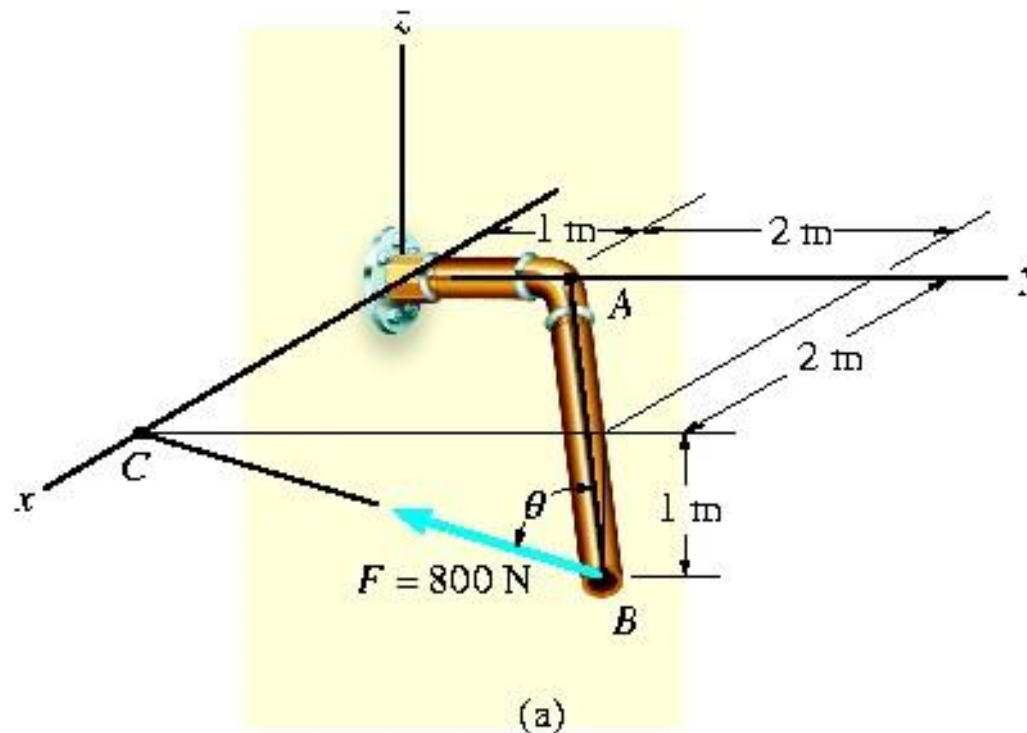
$$\mathbf{A} = \mathbf{A}_\parallel + \mathbf{A}_\perp,$$

then $\mathbf{A}_\perp = \mathbf{A} - \mathbf{A}_\parallel$

$$\begin{aligned} |\vec{F}_\perp| &= \sqrt{|\vec{F}|^2 - |\vec{F}_{AB}|^2} \\ &= \sqrt{(300\text{ N})^2 - (257.1\text{ N})^2} \\ &= 155\text{ N} \end{aligned}$$

Example 2.17

The pipe is subjected to force, $\mathbf{F} = 800 \text{ N}$ at point B. Determine the angle θ between \mathbf{F} and pipe segment BA, and the magnitude of the components of force \mathbf{F} , which are parallel and perpendicular to the member BA



Solution Example 2.17

For angle θ

$$\mathbf{r}_{BA} = \{-2\mathbf{i} - 2\mathbf{j} + 1\mathbf{k}\}\text{m}$$

$$\mathbf{r}_{BC} = \{-3\mathbf{j} + 1\mathbf{k}\}\text{m}$$

Thus,

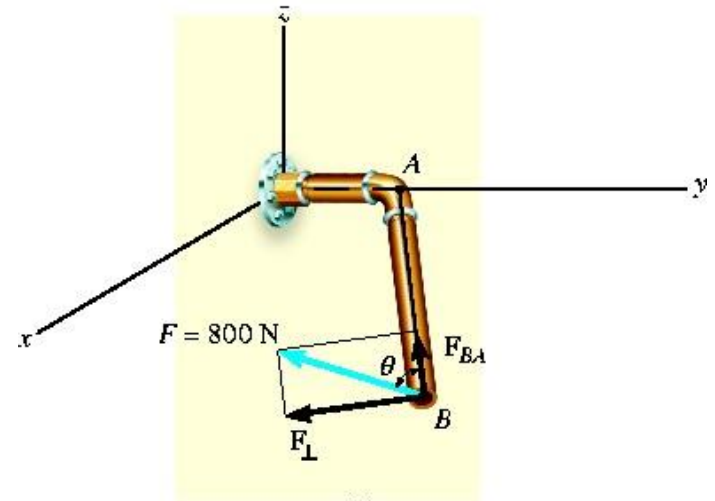
$$\cos \theta = \frac{\vec{r}_{BA} \cdot \vec{r}_{BC}}{|\vec{r}_{BA}| |\vec{r}_{BC}|} = \frac{(-2)(0) + (-2)(-3) + (1)(1)}{3\sqrt{10}}$$

$$= 0.7379$$

$$\theta = 42.5^\circ$$

Express in Cartesian form:

- Parallel component
- Perpendicular component



(b)

$$\vec{u}_{AB} = \frac{\vec{r}_{AB}}{|\vec{r}_{AB}|} = \frac{(-2\vec{i} - 2\vec{j} + 1\vec{k})}{3}$$

$$= \left(-\frac{2}{3}\right)\vec{i} + \left(-\frac{2}{3}\right)\vec{j} + \left(\frac{1}{3}\right)\vec{k}$$

$$|\vec{F}_{AB}| = \vec{F} \cdot \vec{u}_{AB}$$

$$= (-758.9\vec{j} + 253.0\vec{k}) \cdot \left(-\frac{2}{3}\right)\vec{i} + \left(-\frac{2}{3}\right)\vec{j} + \left(\frac{1}{3}\right)\vec{k}$$

$$= 0 + 506.0 + 84.3$$

$$= 590\text{N}$$

Solution Example 2.17

Checking from trigonometry,

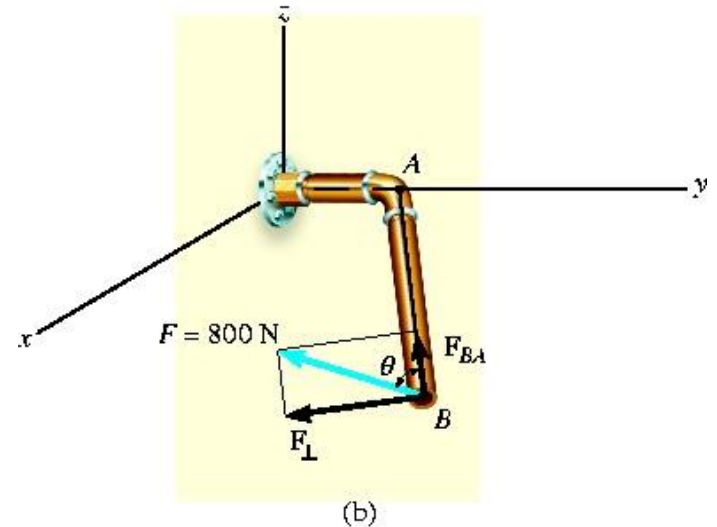
$$\begin{aligned} |\vec{F}_{AB}| &= |\vec{F}| \cos \theta \\ &= 800 \cos 42.5^\circ \text{ N} \\ &= 540 \text{ N} \end{aligned}$$

Magnitude can be determined
From \mathbf{F}_\perp

$$|\vec{F}_\perp| = |\vec{F}| \sin \theta = 800 \sin 42.5^\circ = 540 \text{ N}$$

Magnitude can be determined from \mathbf{F}_\perp
or from Pythagorean Theorem

$$\begin{aligned} |\vec{F}_\perp| &= \sqrt{|\vec{F}|^2 - |\vec{F}_{AB}|^2} \\ &= \sqrt{(800)^2 - (590)^2} \\ &= 540 \text{ N} \end{aligned}$$



Conclusion of The Chapter 2 part III

- Conclusions
 - The Force and Position vector have been identified and determined in the mechanics
 - The Dot Product has been implemented in determine an angle between two vectors



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