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REINFORCED CONCRETE DESIGN 1

Design of Column (Examples and Tutorials) by

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Example 1: Classification of slenderness

Figure 1 show the layout floor view of a building frame, whereas the elevation view is shown in the same figure. The building has reinforced concrete slab from ground floor to the roof floor. The main dimensions, structural features, loads, materials etc. are also set out below.

Calculate the slenderness of the column at B/2 on Ground floor and classify the column whether slender or non-slender (short). The column is considered braced with provision of bracing system at certain location.

Example 1: Classification of slenderness

Column B/2: Ground floor to Level 1

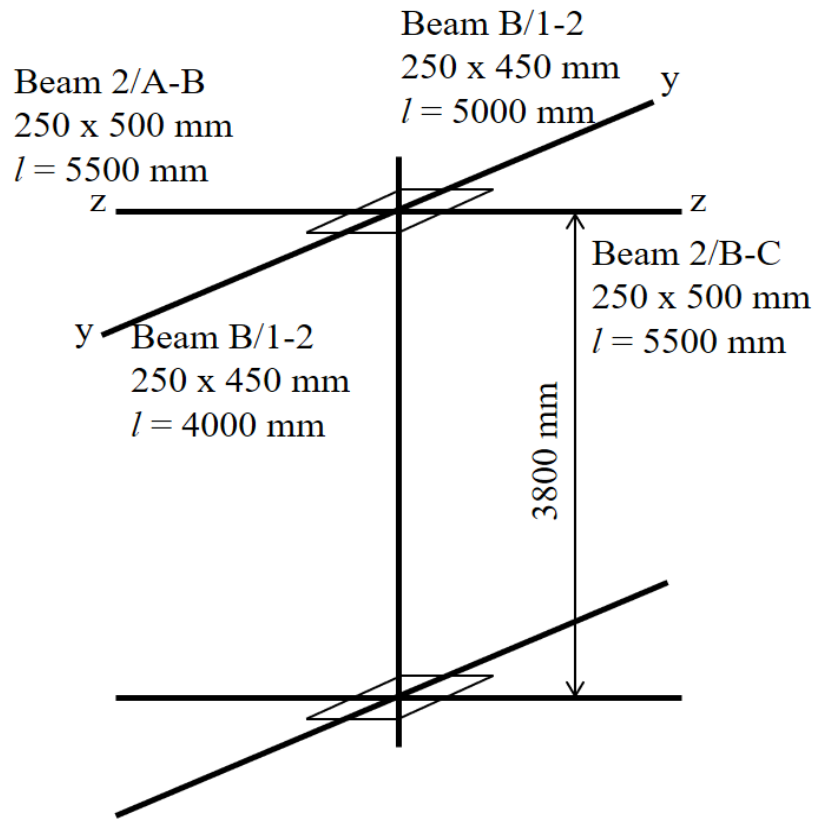


Figure 1

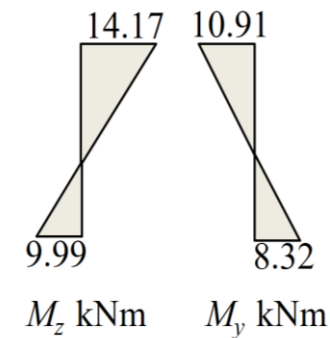
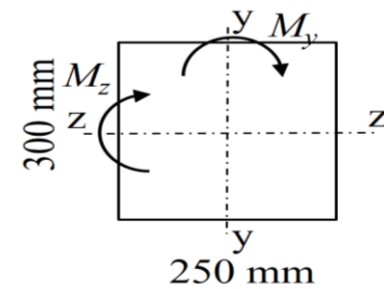
Material,

$$f_{ck} = 25 \text{ N/mm}^2$$

$$f_{yk} = 25 \text{ N/mm}^2$$

$$N_{ed} = 800 \text{ kN}$$

Moments



Example 1: Classification of slenderness

Dimension and size:

Beam:

$$B/1-3, b \times h = 250 \times 450 \text{ mm}$$

$$L_{1-2} = 4.0 \text{ m}$$

$$L_{2-3} = 5.0 \text{ m}$$

$$2/A-C, b \times h = 250 \times 500 \text{ mm}$$

$$L_{A-B} = 5.5 \text{ m}$$

$$L_{B-C} = 5.5 \text{ m}$$

$$\text{Column: } b \times h = 250 \times 300 \text{ mm}$$

$$l_z = 3800 - 450 = 3350 \text{ mm}$$

$$l_y = 3800 - 500 = 3300 \text{ mm}$$

Example 1: Classification of slenderness

Effective length, $l_o = factor \times clear\ height$

x-axis: End condition Top = 1 Beam at both sides, $h_b > h_c$
 Bot = 1 450 > 300

Factor = 0.75

$$l_o = 0.75 \times 3350 = 2513 \text{ mm}$$

y-axis: End condition Top = 1 Beam at both sides, $h_b > h_c$
 Bot = 1 500 > 250

Factor = 0.75

$$l_o = 0.75 \times 3300 = 2475 \text{ mm}$$

Example 1: Classification of slenderness

Radius of gyration = $(I/A)^{1/2}$

$$i_z = (5.63 \times 10^8 / 75000)^{1/2} = 87 \text{ mm}$$

$$i_y = (3.91 \times 10^8 / 75000)^{1/2} = 72 \text{ mm}$$

Slenderness ratio, $\lambda = l_0/i$

$$\lambda_z = 2513 / 87 = 28.9$$

$$\lambda_y = 2475 / 72 = 34.4$$

Slenderness limit, $\lambda_{lim} = 20.A.B.C/n^{1/2}$

$$A = 1/(1 + 0.2\varphi_{eff}) = 0.7 \quad (\varphi_{eff} \text{ not known})$$

$$B = (1 + 2\omega)^{0.5} = 1.1 \quad (\omega \text{ not known})$$

$$C = 1.7 - r_m \quad \text{where } r_m = M_{o1}/M_{o2}$$

$$\text{z-axis: } r_m = 9.99 / 14.17 = 0.71$$

$$C_z = 1.7 - 0.71 = 0.99$$

$$\text{y-axis: } r_m = 8.32 / 10.91 = 0.76$$

$$C_y = 1.7 - 0.76 = 0.94$$

Example 1: Classification of slenderness

$$n = N_{Ed} / (A_c f_{cd})$$

$$A_c = 250 \times 300 = 75000 \text{ mm}^2$$

$$f_{cd} = 0.85 f_{ck} / \gamma_c = 0.85 \times 25 / 1.5 = 14.17 \text{ N/mm}^2$$

$$n = 888.91 \times 10^3 / (75000 \times 14.17)$$

$$= 0.84$$

$$\text{z-axis: } \lambda_{lim,z} = 20 \times 0.7 \times 1.1 \times 0.99 / (0.84)^{1/2}$$

$$= 16.6 < \lambda_z = 28.9$$

Slender column

$$\text{y-axis: } \lambda_{lim,y} = 20 \times 0.7 \times 1.1 \times 0.94 / (0.84)^{1/2}$$

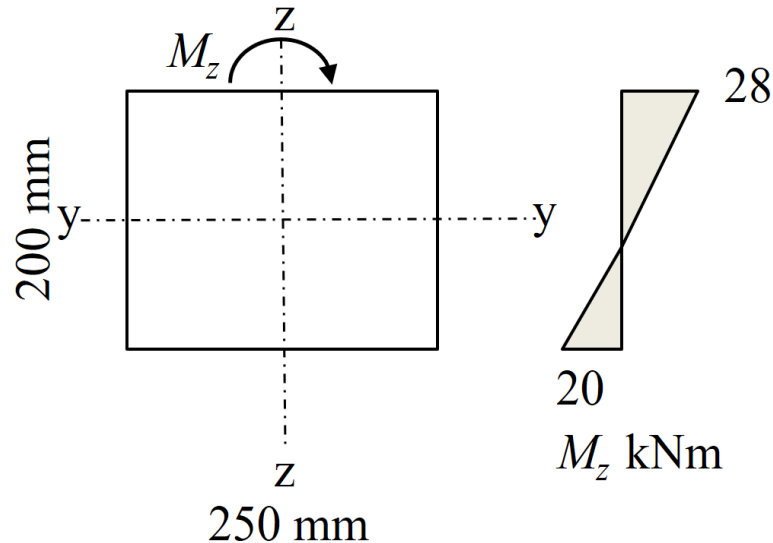
$$= 15.8 < \lambda_y = 34.4$$

Slender column

Example 2: Short braced column bent about major axis

Design the longitudinal and transverse reinforcement of 200 x 250 mm column with 800kN ultimate axial load and bending moment values as shown in figure below. The moment is determined to bent about major axis with effective length of 3.1 m. This column is classified as non-slender column some bracing system in the frame. Specification of the structure is given as follows:
Exposure class XC1, Fire resistance = 1 hour, Design life 50 years. Consider concrete grade of C25/30 and steel reinforcement grade of 500.

Example 2: Short braced column bent about major axis



Assumed: $\phi_{link} = 6 \text{ mm}$

$\phi_{bar} = 20 \text{ mm}$

Example 2: Short braced column bent about major axis

DURABILITY, BOND AND FIRE RESISTANCE

Min. cover with regard to bond, $C_{\min,b} = 20 \text{ mm}$

Min. cover with regard to durability, $C_{\min,b} = 15 \text{ mm}$

Min. required axis distance for R60 fire resistance

$$a_{sd} = 36 \text{ mm}$$

Min. concrete cover with regard to fire,

$$C_{\min} = a_{sd} - \phi_{link} - \phi_{bar}/2 = 36 - 6 - 20/2 = 20 \text{ mm}$$

Allowance in design for deviation, $\Delta C_{dev} = 10 \text{ mm}$

Nominal cover,

$$C_{\text{nom}} = C_{\min} + \Delta C_{dev} = 20 + 10 = 30 \text{ mm}$$

Use: $C_{\text{nom}} = 30 \text{ mm}$

Example 2: Short braced column bent about major axis

DESIGN MOMENT

For non-slender column the design moment,

$$M_{Ed} = \text{Max}\{M_{02}, M_{min}\}$$

where,

$$M_{02} = M + N_{Ed} \cdot e_i$$
$$M = \text{Max}\{|M_{top}|, |M_{bot}|\} = 28 \text{ kNm}$$
$$e_i = l_o/400 = 3100 / 400 = 7.8 \text{ mm}$$
$$M_{02} = 28 + (800 \times 0.0078) = 34.24 \text{ kNm}$$

$$M_{min} = N_{Ed} \cdot e_o$$
$$e_o = 250 / 30 = 8.3 \text{ mm} \geq 20 \text{ mm}$$
$$M_{min} = 800 \times 0.02 = 16 \text{ kNm}$$

$$\rightarrow M_{Ed} = 34.24 \text{ kNm}$$

Example 2: Short braced column bent about major axis

REINFORCEMENT

$$d_2 = C_{nom} + \phi_{link} + \phi_{bar}/2 = 30 + 6 + 20/2 = 46 \text{ mm}$$

$$d_2/h = 46 / 250 = 0.18 \text{ (Use chart 0.2)}$$

$$\begin{aligned} N / bhf_{ck} &= 800 \times 10^3 / (200 \times 250 \times 25) \\ &= 0.64 \end{aligned}$$

$$\begin{aligned} M / bh^2f_{ck} &= 34.24 \times 10^6 / (200 \times 250^2 \times 25) \\ &= 0.11 \end{aligned}$$

$$A_s f_{yk} / bhf_{ck} = 0.53$$

$$\begin{aligned} A_s &= 0.53 bhf_{ck} / f_{yk} \\ &= 0.53 (200 \times 250 \times 25) / 500 \\ &= 1325 \text{ mm}^2 \end{aligned}$$

Example 2: Short braced column bent about major axis

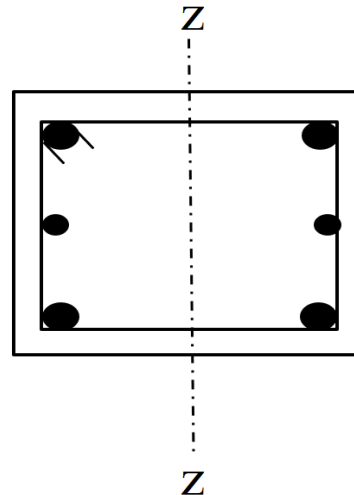
$$\begin{aligned}A_{min} &= 0.1 N_{Ed} / f_{yd} = 0.1 N_{Ed} / (0.87 f_{yk}) \\ &= 0.1 \times 800 \times 10^3 / (0.87 \times 500) \\ &= 184 \text{ mm}^2 \quad \text{or} \quad 0.002 A_c = 100 \text{ mm}^2\end{aligned}$$

$$A_{max} = 0.04 A_c = 2000 \text{ mm}^2$$

Use:

4H20 + 2H12

(1483 mm²)



Example 2: Short braced column bent about major axis

Links, ϕ_{min} = the larger of
 $= 0.25 \times 20 = 5 \text{ mm}$
or 6 mm

$S_{v,max}$ = the lesser of
 $= 20 \times 12 = 240 \text{ mm}$
or 200 mm
or 400 mm Use: H6 – 200

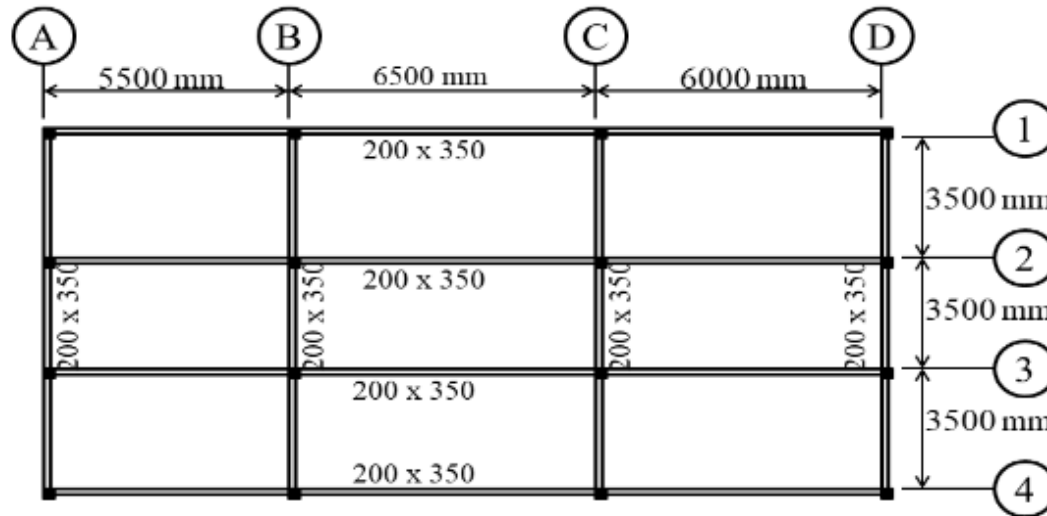
At section 250 mm below and above beam and at lapped joints, $S_{v,max} = 0.6 \times 200 = 120 \text{ mm}$

Use: H6 – 120

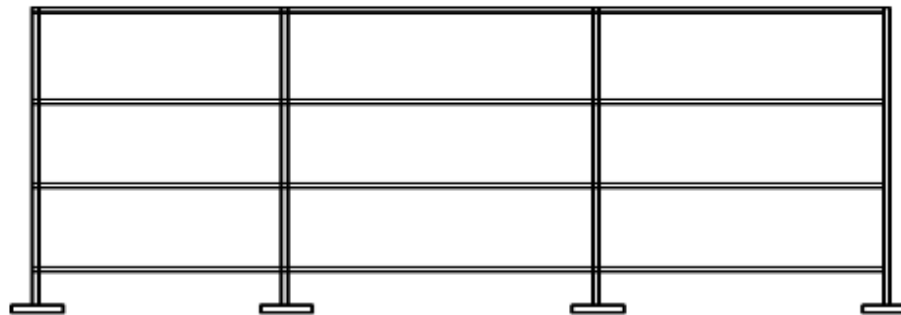
Tutorial 1: Column slenderness

Figure 2 shows a plan view and cross-section view of a three-storey reinforced concrete building. The building is considered braced with the provision of bracing elements at certain locations. The size of the column is designed to be 250 x 250 mm, whereas the size of the beam is taken as 200 x 350 mm. The height of each floor is 3.6 m. Calculate the slenderness of the column at D/4 on the 1st Floor and classify the column whether slender or non-slender (short).

Tutorial 1: Column slenderness



Plan view



Cross-section view

Figure 2

Tutorial 2: Short column uniaxial bending

A rectangular column carries an ultimate moment of 33 kNm bend about minor axis. The column effective height is 3.55 m with a cross-section area of 250 mm x 300 mm. This column is classified as non-slender column and is subjected to ultimate axial load of 1150 kN. The column is to be designed for 1 hour fire resistance and at least 50 years design life. The exposure class considered is XC1.

Tutorial 2: Short column uniaxial bending

- a) By using C25/30 grade concrete and steel reinforcement grade of 500, calculate the design moment for the column bend about minor axis. Assume that the diameter of the main bar and link is 20 mm and 6 mm, respectively.
- b) Calculate and design the longitudinal and shear reinforcement required for the column. Comment on your answer and give appropriate suggestions.
- c) Construct detail of the reinforcement (longitudinal and shear reinforcement) obtained in (b) for the column.

End of Examples and Tutorials