

MECHANICS OF MATERIALS

Analysis of Strain

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Chapter Description

- **Expected Outcomes**
 - Identify the concepts of strain.
 - Apply the concept of strain in calculating the normal and shear strain in the body.
 - Calculate the deformation in the body.

1.1 Deformation

- **Strain:** a force or influence that stretches, pulls, or puts pressure on something, sometimes **causing damage**
- **Deformation:** When a **force** is applied to a body, it will change the body's **shape** and **size**
- Eg: A rubber band – will undergo a very large deformation when stretched
- Excessive stress in brittle materials such as concrete has caused it to strain until it fractured
- **Load** will cause all material bodies to **deform**

1.2 Strain

- Strain- the relative **change** in **shape** or **size** of an object due to externally-applied **forces**
- Strain describe the deformation in 2 ways:
 1. Normal strain (ϵ) - epsilon
 2. Shear strain (γ) - gamma

Normal Strain

- Normal Strain- deformation of the member per unit **length**
 - Deformation -> The **elongation** (+) / **contraction** (-)
- Average normal strain is defined as:

$$\epsilon_{avg} = \frac{\Delta s' - \Delta s}{\Delta s}$$

Δs = Original length

$\Delta s'$ = Final length

$$\epsilon = \frac{\delta}{L} = \text{normal strain}$$

δ = Deformation

L = Length

- If the **normal strain is known**, then the approximate final length is

$$\Delta s' \approx (1 + \varepsilon) \Delta s$$

- Normal strain is a **dimensionless** quantity since it is a **ratio** of two lengths

Shear Strain

- Change in **angle** that occurs between two small line segments that are originally perpendicular to one another

$$\gamma_{nt} = \frac{\pi}{2} - \lim_{\substack{B \rightarrow A \text{ along } n \\ C \rightarrow A \text{ along } t}} \theta'$$

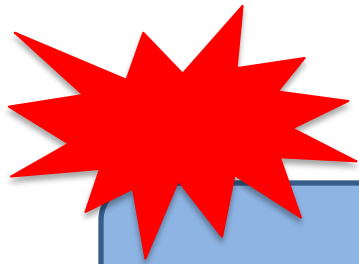
$\theta < 90 \rightarrow$ +shear strain

$\theta > 90 \rightarrow$ -shear strain



REMEMBER

NORMAL STRAIN - Δ LENGTH
SHEAR STRAIN - Δ ANGLE



STRESS

Force / Unit Area

Normal
Stress (σ)

Shear
Stress (τ)

STRAIN

Measure of Deformation

Normal
Strain (ϵ)

Shear
Strain (γ)

References

- Hibbeler, R.C., Mechanics Of Materials, 9th Edition in SI units, Prentice Hall, 2013.
- Ferdinand P. Beer, E. Russell Johnston, Jr., John T. DeWolf, David F. Mazurek, Mechanics of materials 5th Edition in SI Units, McGraw Hill, 2009.

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