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# THEORY OF STRUCTURES

## CHAPTER 4 : TRUSSES (METHOD OF JOINT)

### PART 1

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# Chapter 4 : Part 1 – Method of Joint

- Aims
  - Determine internal forces in truss member
- Expected Outcomes :
  - Able to analyse trusses using method of joint
- References
  - Mechanics of Materials, R.C. Hibbeler, 7th Edition, Prentice Hall
  - Structural Analysis, Hibbeler, 7th Edition, Prentice Hall
  - Structural Analysis, SI Edition by Aslam Kassimali, Cengage Learning
  - Structural Analysis, Coates, Coatie and Kong
  - Structural Analysis - A Classical and Matrix Approach, Jack C. McCormac and James K. Nelson, Jr., 4th Edition, John Wiley



# INTRODUCTION TO TRUSS

- TRUSS – structure composed of slender member joined together at their end points
- Commonly construct consist of wooden struts and metal bars (steel)
- Connection joints – by bolting or welding to gusset plate  
Objective : To determine the reactions and member forces
- Three methods to carry out the analysis of statically determinate trusses
  - Method of Joints
  - Method of Section
  - Unit Load Method



# ANALYSIS OF STATICALLY DETERMINATE PLANE TRUSSES USING

## PART 1 \*METHOD OF JOINTS\*



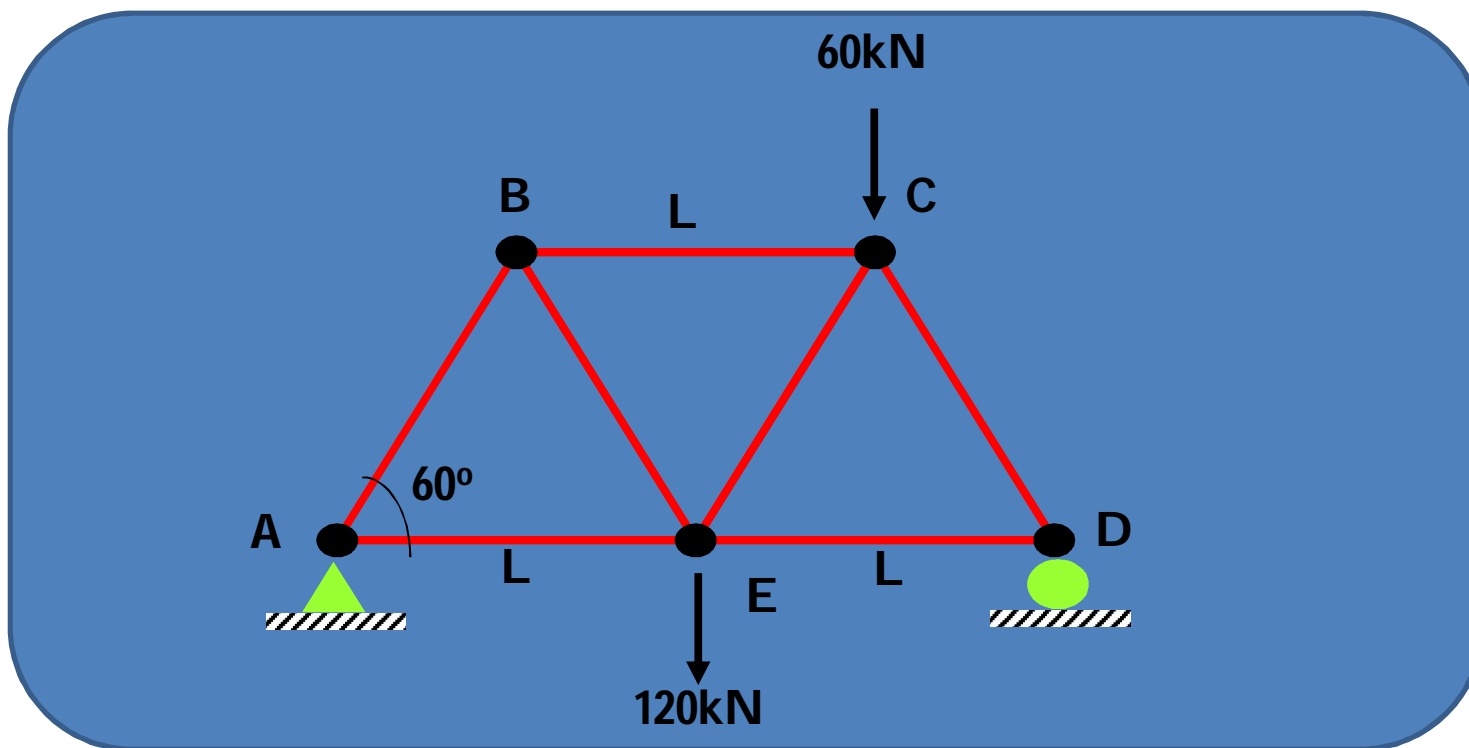
# METHOD OF JOINTS

Simple guidelines for analysis:

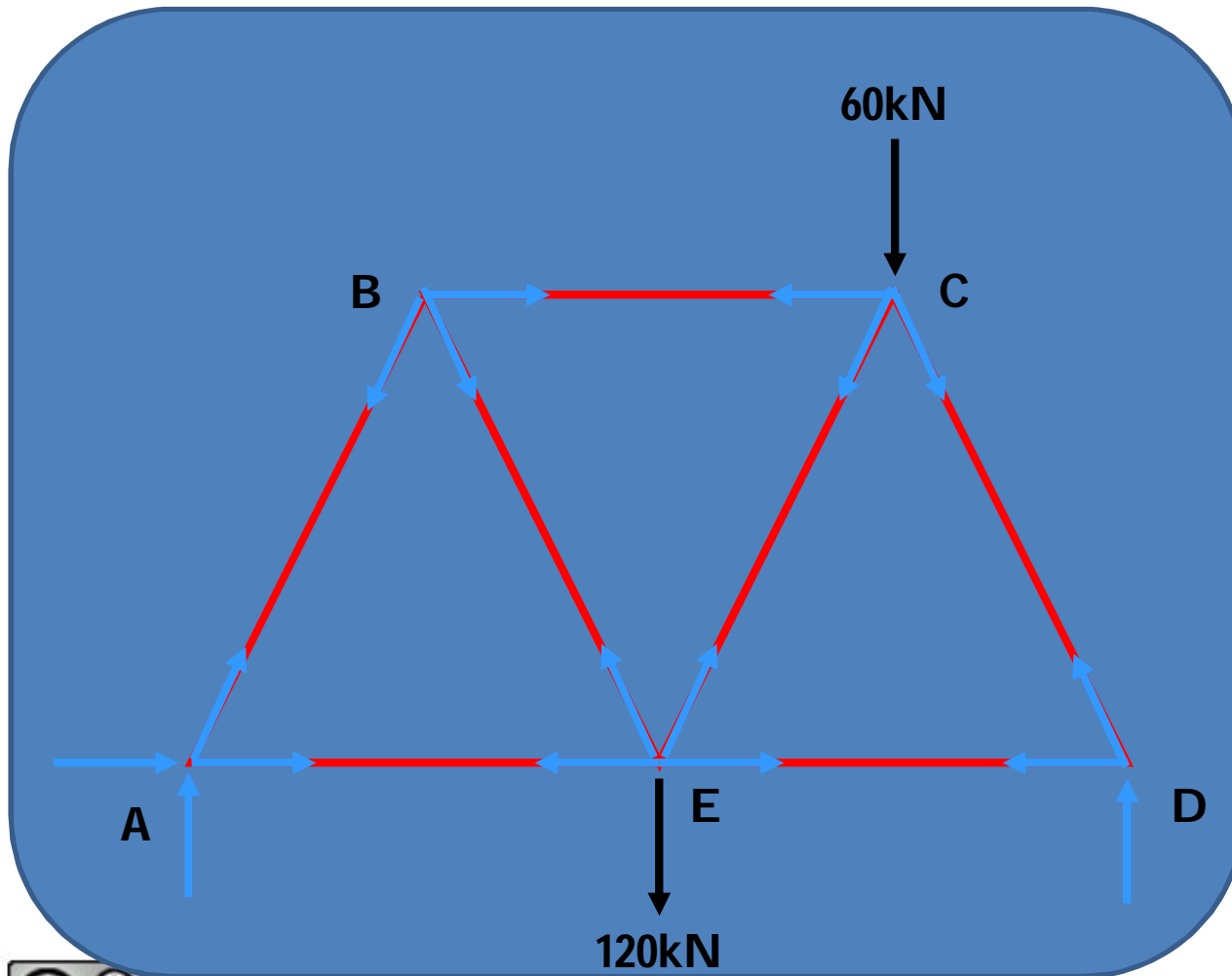
1. Draw the FBD
2. Solve reactions
3. Select joint with minimum number of unknowns  
**(preferably only 2 unknowns)**
4. Analyze magnitude of forces using equilibrium equation
5. Proceed to other joints, concentrating with joints that has minimum no. of unknowns
6. Check member forces at unused joint/ s
7. Tabulate the value of member forces tension (+) and compression (-)

# EXAMPLE 1

Using method of joints, determine the force in each member of the trusses shown (assume  $L = 1\text{m}$ ).



## Free Body Diagram (FBD)



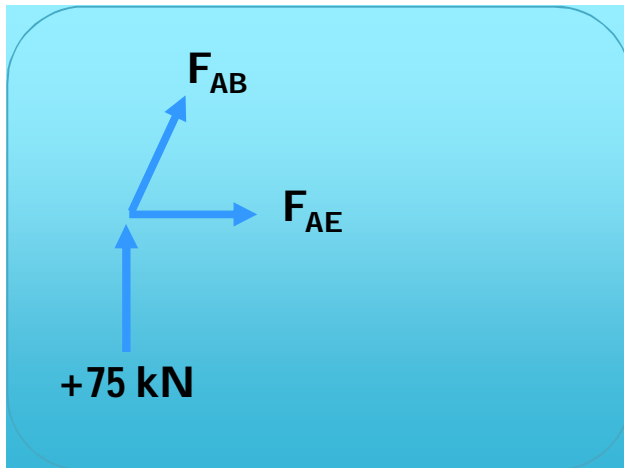
Find Reaction:

$$R_A = 75 \text{ kN}$$

$$R_D = 105 \text{ kN}$$

$$H_A = 0$$

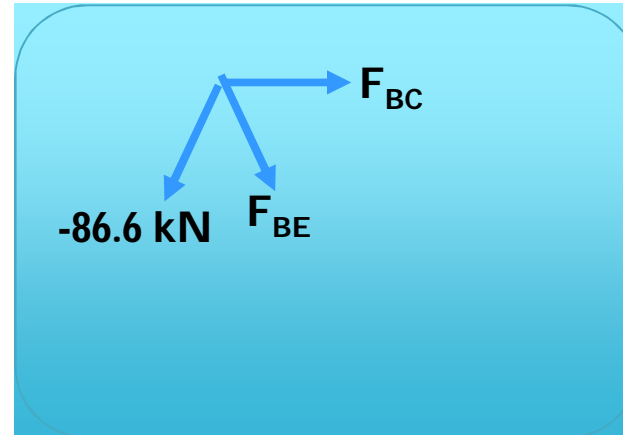
## Joint A



$$\begin{aligned}\sum F_y = 0, \\ 75 + F_{AB} \sin 60 &= 0 \\ F_{AB} &= \underline{\underline{-86.6 \text{ kN}}}\end{aligned}$$

$$\begin{aligned}\sum F_x = 0, \\ F_{AE} + F_{AB} \cos 60 &= 0 \\ F_{AE} + (-86.6) \cos 60 &= 0 \\ F_{AE} &= \underline{\underline{+43.3 \text{ kN}}}\end{aligned}$$

## Joint B

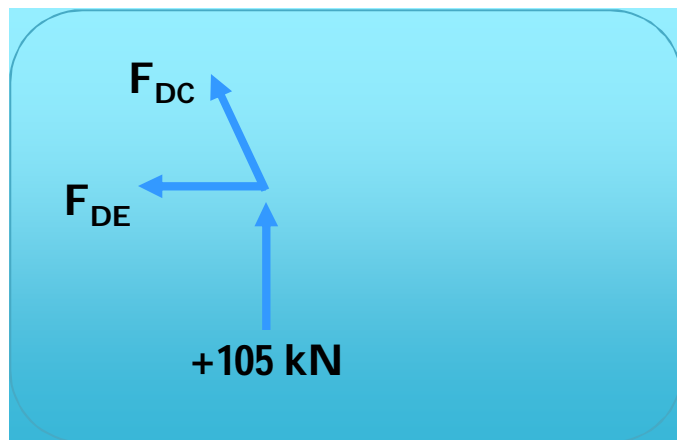


$$\begin{aligned}\sum F_y = 0, \\ -F_{BE} \sin 60 - (-86.6 \sin 60) &= 0 \\ F_{BE} &= \underline{\underline{+86.6 \text{ kN}}}\end{aligned}$$

$$\begin{aligned}\sum F_x = 0, \\ F_{BC} - (-86.6 \cos 60) + F_{BE} \cos 60 &= 0 \\ F_{BC} + 86.6 \cos 60 + 86.6 \cos 60 &= 0 \\ F_{BC} &= \underline{\underline{-86.6 \text{ kN}}}\end{aligned}$$



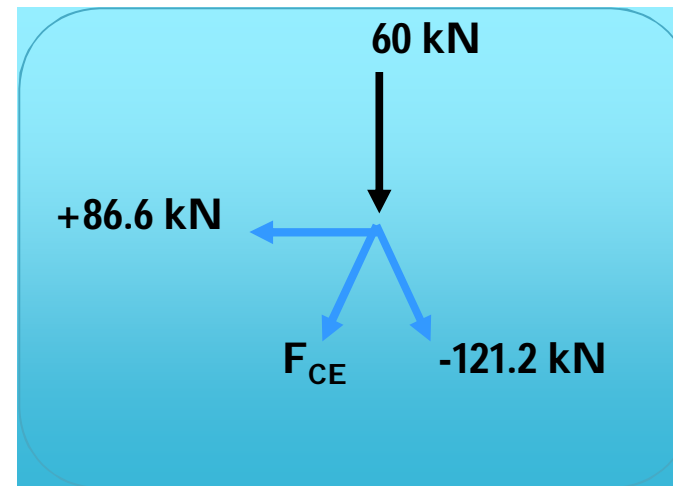
## Joint D



$$\begin{aligned}\sum F_y &= 0, \\ 105 + F_{DC} \sin 60 &= 0 \\ F_{DC} &= \underline{\underline{-121.2 \text{ kN}}}\end{aligned}$$

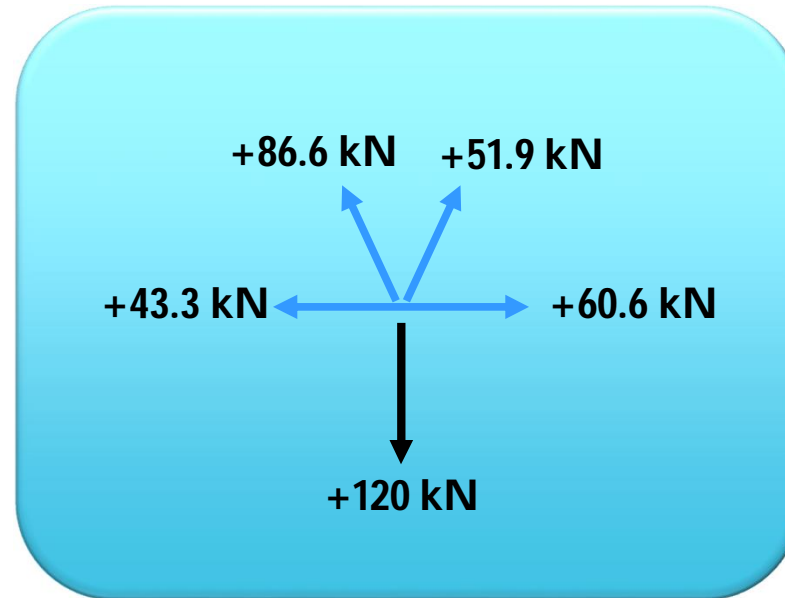
$$\begin{aligned}\sum F_x &= 0, \\ -F_{DE} - F_{DC} \cos 60 &= 0 \\ -F_{DE} - (-121.2 \cos 60) &= 0 \\ F_{DE} &= \underline{\underline{+60.6 \text{ kN}}}\end{aligned}$$

## Joint C



$$\begin{aligned}\sum F_y &= 0, \\ -60 - (-121.2 \sin 60) - F_{CE} \sin 60 &= 0 \\ F_{CE} &= \underline{\underline{+51.9 \text{ kN}}}\end{aligned}$$

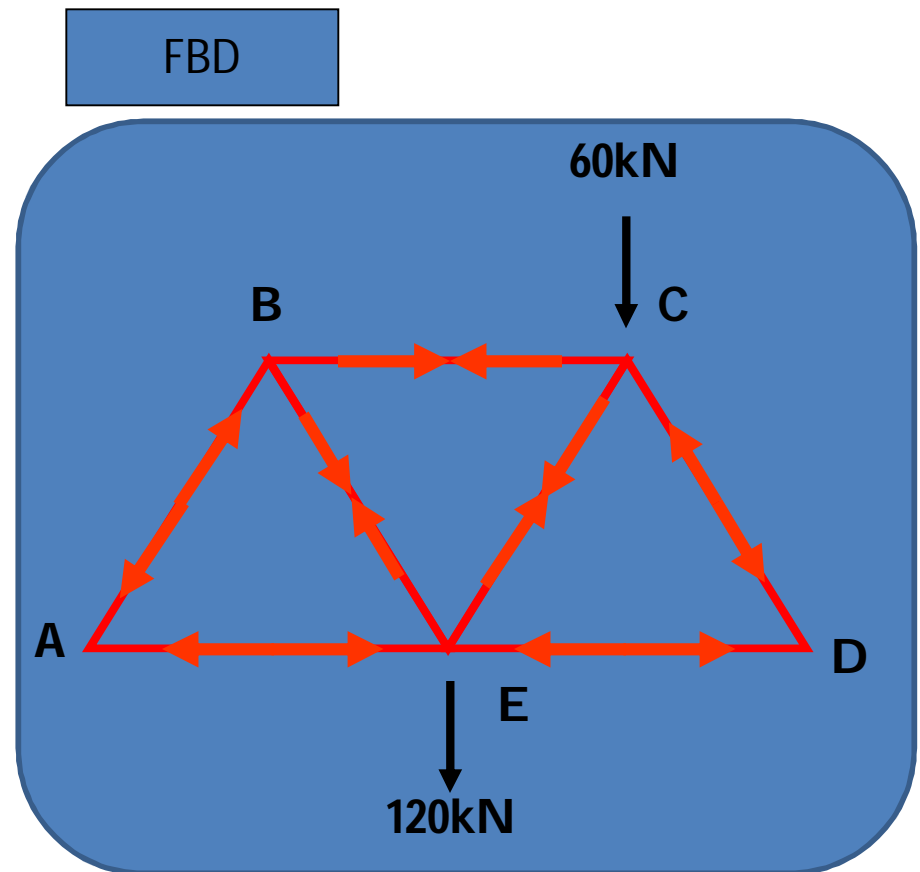
## Checking at Joint E



$$\begin{aligned} \sum F_x &= 0, \\ -43.3 - 86.6 \cos 60 + 51.9 \cos 60 + 60.6 &= 0 \\ &0 = 0 \dots \text{(OK)} \end{aligned}$$

$$\begin{aligned} \sum F_y &= 0, \\ -120 + 86.6 \sin 60 + 51.9 \sin 60 &= 0 \\ &0 = 0 \dots \text{(OK)} \end{aligned}$$

Member	Force (kN)	Condition
AB	- 86.6	Comp.
BC	-86.6	Comp.
CD	- 121.2	Comp.
DE	+ 60.6	Tension
EA	+ 43.3	Tension
BE	+ 86.6	Tension
CE	+ 51.9	Tension



# THANKS



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