

# BIOREACTOR ENGINEERING

## Chapter 3

### Culture Kinetic Study of Continuous Fermentation

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Culture Kinetic Study of Continuous Fermentation by Chew Few Ne

# Chapter Description

- Topic Outcome
  - Perform calculation regarding culture kinetics of continuous fermentation
- References
  - Doran, P.M. (2013) Bioprocess Engineering Principles. Elsevier.
  - Liu, S. (2013) Bioprocess Engineering: Kinetics, Biosystem, Sustainability and Reactor Design. Elsevier.
  - Rao, D.G. (2010) Introduction to Biochemical Engineering. McGraw Hill.



# Topic Outline

- Kinetics of Cell Growth
- Kinetics of Substrate Consumption
- Kinetics of Product Formation



# Kinetics of Cell Growth

- Material balance around the chemostat on the cell:

Cell accumulation = cell in – cell out + cell growth – cell death

Please write the formula = ?

$F$  = volumetric flow rate of medium (feed & effluent) (L/h)

$S_0$  = substrate concentration in the feed (g/L)

$X_0$  = cell concentration in the feed (g/L)

$P_0$  = product concentration in the feed (g/L)

$S$  = substrate concentration in the fermenter (g/L)

$X$  = cell concentration in the fermenter (g/L)

$P$  = product concentration in the fermenter (g/L)

$V$  = liquid volume of fermenter (L)

$\mu$  = specific growth rate ( $\text{h}^{-1}$ )

$k_d$  = specific death rate ( $\text{h}^{-1}$ )



# Kinetics of Cell Growth

- For single-stage chemostat, medium supply is usually sterile
- During exponential phase:  $k_d \ll \mu \rightarrow k_d \approx 0$
- So, 
$$\frac{dX}{dt} = -\frac{F}{V}X + \mu X$$
- Let dilution rate, D: 
$$D = \frac{\text{medium flowrate}}{\text{culture volume}} = \frac{F}{V}$$
- So, Please write the formula = ?
- During steady state, 
$$\frac{dX}{dt} = 0 \quad \therefore \mu = D$$
- The equation shows that by varying the medium supply rate, the growth rate can be varied



# Kinetics of Cell Growth

- From Monod equation:

$$\mu = \mu_{max} \frac{S}{K_S + S}$$

- Thus,

$$D = \mu_{max} \frac{S}{K_S + S}$$

OR

$$S = \frac{K_S D}{\mu_{max} - D}$$



# Kinetics of Cell Growth

- Exercise 1



# Kinetics of Substrate Consumption

- Material balance around the chemostat on the limiting substrate:

substrate accumulation = substrate in – substrate out – substrate for growth – substrate for product formation – substrate for maintenance

Please write the formula = ?

$F$  = volumetric flow rate of medium (feed & effluent) (L/h)

$V$  = liquid volume of fermenter (L)

$S_0$  = limiting substrate concentration in the feed (g/L)

$S$  = limiting substrate concentration in the fermenter (g/L)

$Y_{x/S}$  = the theoretical yield of cell from substrate (g cell dry weight formed per g substrate consumed)

$Y_{p/S}$  = the theoretical yield of product from substrate (g product formed per g substrate consumed)

$\mu$  = specific growth rate ( $\text{h}^{-1}$ )

$q_p$  = specific product formation rate ( $\text{h}^{-1}$ ).

$m$  = the maintenance coefficient (g substrate consumed per g cell dry weight per hour)





# Kinetics of Substrate Consumption

- In general,  $mX \ll \frac{\mu X}{Y_{X/S}}$  and can be neglected
- If no product is formed, so: Please write the formula = ?
- During steady state,  $\frac{dS}{dt} = 0$  and  $\frac{F}{V} = D$
- So:  $X = Y_{X/S}(S_0 - S)$
- With  $S = \frac{K_S D}{\mu_{max} - D} \rightarrow X = Y_{X/S} \left( S_0 - \frac{K_S D}{\mu_{max} - D} \right)$



# Kinetics of Substrate Consumption

- From the graph of cell and substrate concentration as a function of dilution rate,
  - At low  $D$ , all the substrate is consumed at steady state,  $S \approx 0$  and  $X$  is high:  
high:  $X = Y_{X/S} S_0$
  - As  $D$  increases,  $S$  increases and  $X$  decreases.
- For  $X$  falls to zero rapidly,
  - This is called a washout condition.
  - The rate at which cells are removed in the outlet stream is greater than the rate of generation by growth.
  - Although  $\mu$  can be manipulated by changing  $D$ , the cell growth rate is ultimately limited to  $\mu_{\max}$
  - During washout,  $D = D_c$  (critical dilution rate)



# Kinetics of Substrate Consumption

- To calculate the value of  $D_c$ , from previous:

$$D = \mu_{max} \frac{S}{K_s + S}$$

- If  $D = D_c$ ,  $S = S_0$  when  $X = 0$ , and  $K_s \ll S_0$

- So,  $D_c = \mu_{max}$

- We must avoid washout in practical operation where  $D < D_c$
- When the  $D \approx D_c$ , small changes in  $D$  cause large changes in  $X$  and  $S$  (due to fluctuation in the flow rate).



# Kinetics of Product Formation

- The cell productivity of a chemostat:  $P_X = DX$

$P_X$  = volumetric rate of cell production (g/L.h)

$D$  = dilution rate ( $\text{h}^{-1}$ )

$X$  = cell concentration (g/L)

- From previous:

$$X = Y_{X/S} \left( S_0 - \frac{K_S D}{\mu_{max} - D} \right)$$

- So,  $P_X = D Y_{X/S} \left( S_0 - \frac{K_S D}{\mu_{max} - D} \right)$



# Kinetics of Product Formation

- From the graph of cell productivity as a function of dilution rate, the dilution rate giving rise to maximum productivity,  $D_{opt}$  can be calculated by solving:

$$\frac{dP_X}{dD} = 0$$

- So, 
$$D_{opt} = \mu_{max} \left( 1 - \sqrt{\frac{K_S}{K_S + S_0}} \right)$$

- If  $K_S \ll S_0$ ,  $D_{opt} \approx \mu_{max} \approx D_c$  (Washout may occur)



# Kinetics of Product Formation

- Exercise 2



# CREDITS

Special thanks to

- Prof. Dr. Tey Beng Ti
- Prof. Madya Dr. Rosfarizan binti Mohamad
- Dr. Farhan binti Mohd Said

Thanks to Dr. Rozaimi bin Abu Samah for proofreading the learning contents.

